



# Spectroscopic Ellipsometry for Thin Film Characterization Theory & Fundamentals

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## PRESENTATION OVERVIEW

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- Ellipsometry technique : capabilities and advantages
- Ellipsometry definition
- Light and polarization
- Optical constants
- Reflection with films
- EMA theory
- Analysis of ellipsometric data
- Phase Modulation Ellipsometer: How does it work ?
- Basic ellipsometer operations: choice of spectral range, angle of incidence

# **HORIBA**JOBIN YVON A Global Company

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- **Creation of Jobin Yvon in 1819**
- **Leader company in spectroscopy and analytical instrumentation**
  - Headquarters: France (20 km from Paris)
  - 300 employees - 3 manufacturing plants in France
  - 5 divisions: Molecular & Micro analysis (Raman, fluorescence), elemental analysis, optical components (gratings, spectrometers, monochromators), particle size, emerging business (ellipsometry, process control, forensics)
- **1997: Jobin Yvon merged into HORIBA Group**
  - More than 4400 employees
  - Annual sales: \$935,000,000
  - 5 segments: ATS, Semiconductor, P&E, Medical, Scientific
- **2004: Jobin Yvon becomes HORIBA Jobin Yvon**

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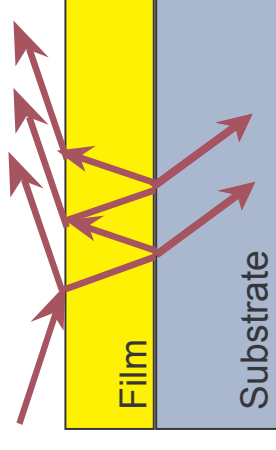
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# General Overview of the Thin Film Division

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- **Development and manufacture of optical metrology systems for**

- ⇒ Characterization of thin films, surfaces and interfaces
  - Laser and Spectroscopic Ellipsometers from FUV to NIR
  - Combined Ellipsometry and Reflectometry



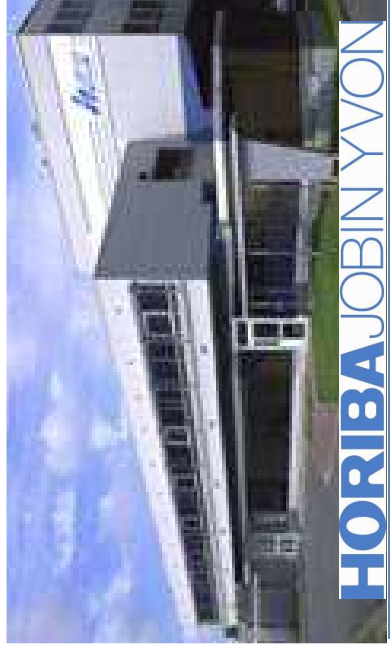
- ⇒ In-situ Process Control of thin film etching and deposition
  - Laser and Polarized Interferometry
  - Optical Emission Spectroscopy

- **Thin Film Division**

- 55 persons (sales, manufacturing, R&D)
- Headquarters: France (20 km from Paris)
- 4 application laboratories worldwide (USA, France, Germany, Japan)

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Welcome to



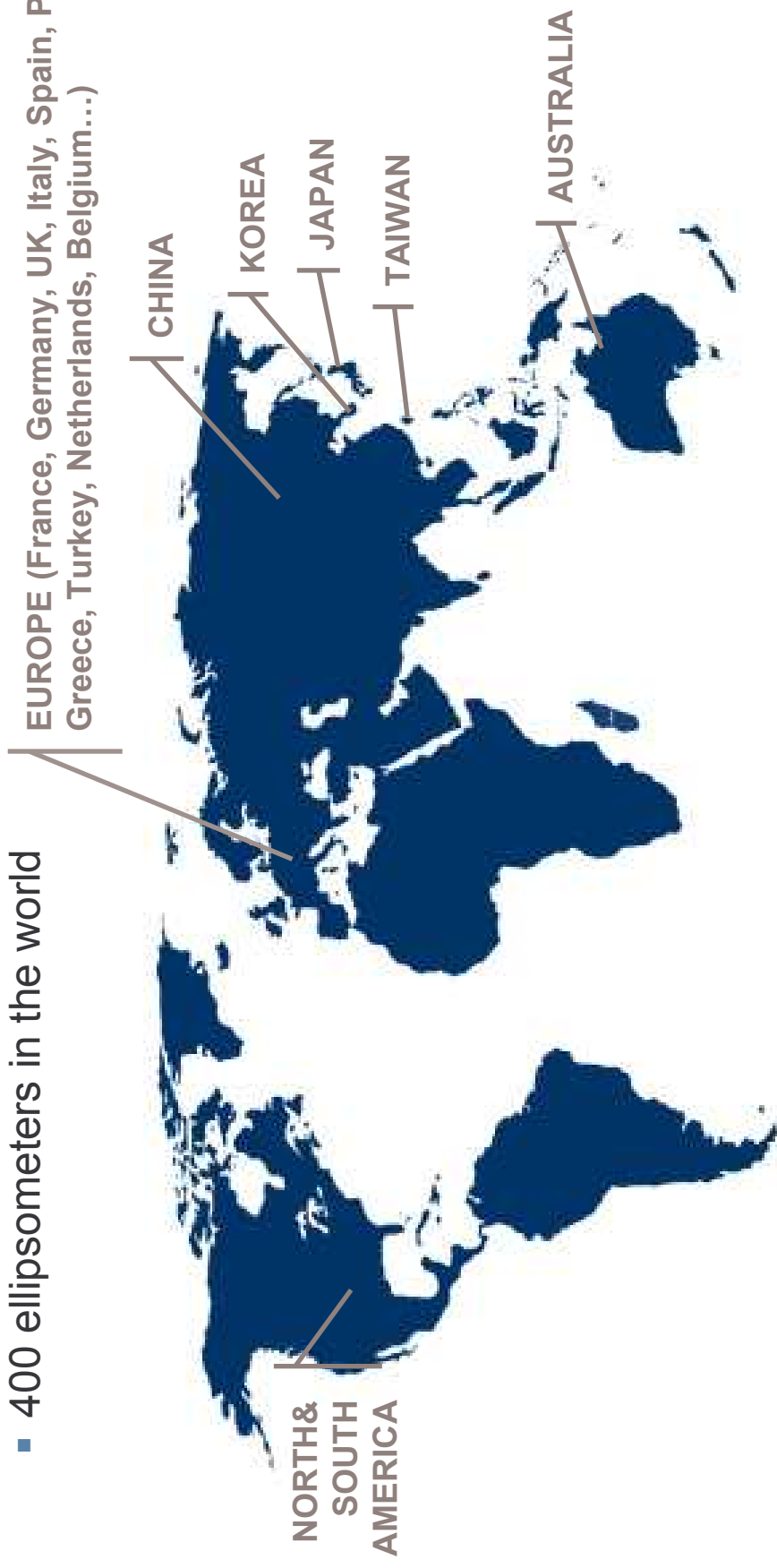
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# User Profile of HORIBA Jobin Yvon Ellipsometer

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- Universities – R&D: 65 %
- Industry: 35 %
- 400 ellipsometers in the world



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# ELLIPSOMETRY CAPABILITIES

Characterization of thin films, surface and interface

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- **Thickness**
  - Accurate thin film measurement from a few angstroms to several tens of microns
  - Characterization of single layer and complex multilayer stacks
  - Characterization of surface and interface
- **Optical properties**
  - Refractive index ( $n$ ) and extinction coefficient ( $k$ ) from the far-UV to near-IR for complex materials, graded and anisotropic layers
- **Material properties**
  - Alloy composition
  - Microstructure and crystallinity
  - Optical bandgap ( $E_g$ )
  - Film uniformity by area and depth

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## Advantages of the Spectroscopic Ellipsometry Technique

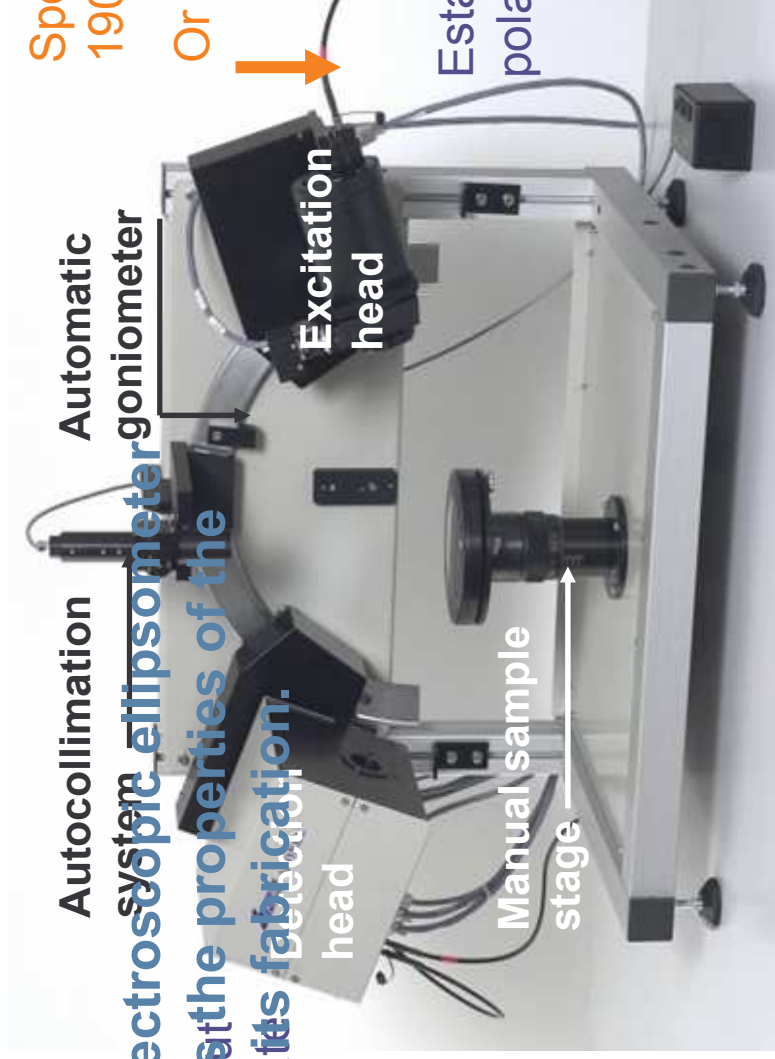
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- Non-destructive & contactless technique
- Highly accurate & reproducible
- Can be used in any transparent and semi-transparent medium
- Very sensitive, especially to ultra-thin films ( $< 10$  nm)
- Spectroscopic measurement: wide spectral range from FUV to NIR
- Simultaneous multiple parameter determination
- Mapping – 2D and 3D cartography
- Pattern measurements

# Ellipsometer Optical Set up



⇒ Ex-situ spectroscopic ellipsometer system  
measures the properties of the sample after fabrication.



The light interacts with the sample and reflects from it. This interaction causes a polarization change of the light.

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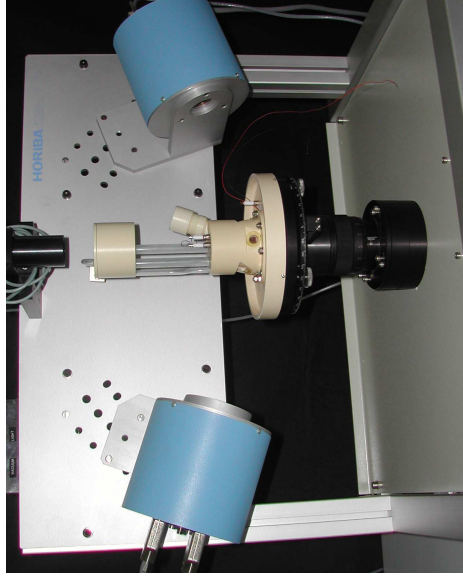
# In Situ Ellipsometry

Real-time monitoring of thin film deposition with submonolayer resolution

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- May be mounted on any process chamber with entrance & exit window
- Real-time calculation of thickness & refractive index of deposited/etched layers
- Accessories: liquid cell, electrochemical cell, thermostated sample stage
- Kinetic measurement of surface modifications during the process



⇒ **In-situ ellipsometry provides the advantage to probe the fabricated structures, to investigate the surface modifications during the process.**

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# Ellipsometry Definition

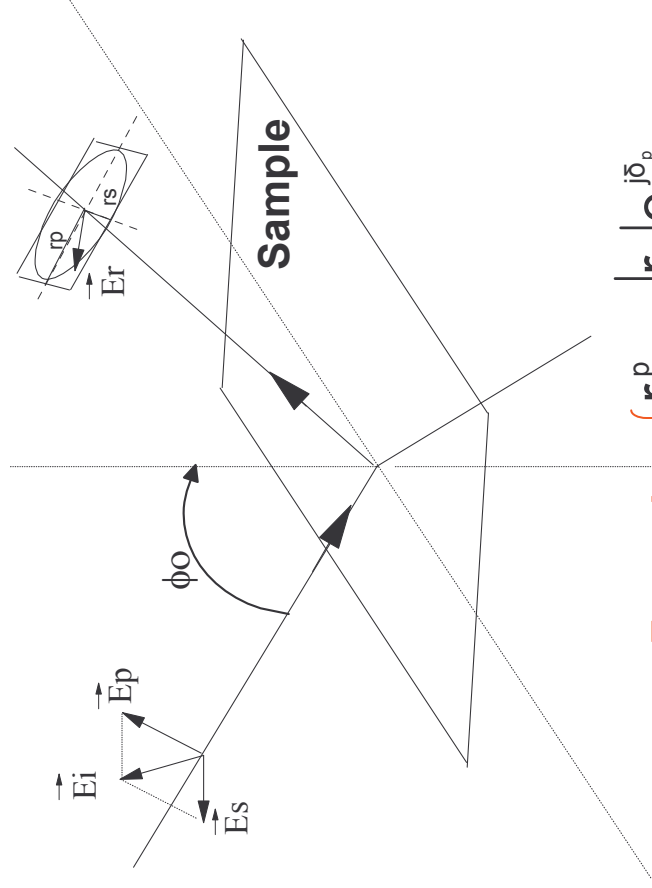
► **Ellipsometry** is an **optical technique** that measures the change in the polarization state of light reflected from the surface of a sample.

$$\frac{r_p}{r_s} = \rho = \tan \psi \exp(i\Delta)$$

>  $\Psi$  and  $\Delta$  : Ellipsometric angles  
Measured data

>  $\tan \psi = \frac{|r_p|}{|r_s|}$  : Amplitude ratio

>  $\Delta = \delta_p - \delta_s$  : Phase shift introduced by reflection from sample



**Fresnel reflection coefficients**

$$\left\{ \begin{array}{l} r_{01}^p = |r_p| e^{j\delta_p} \\ r_{01}^s = |r_s| e^{j\delta_s} \end{array} \right.$$

# Ellipsometry Measurements

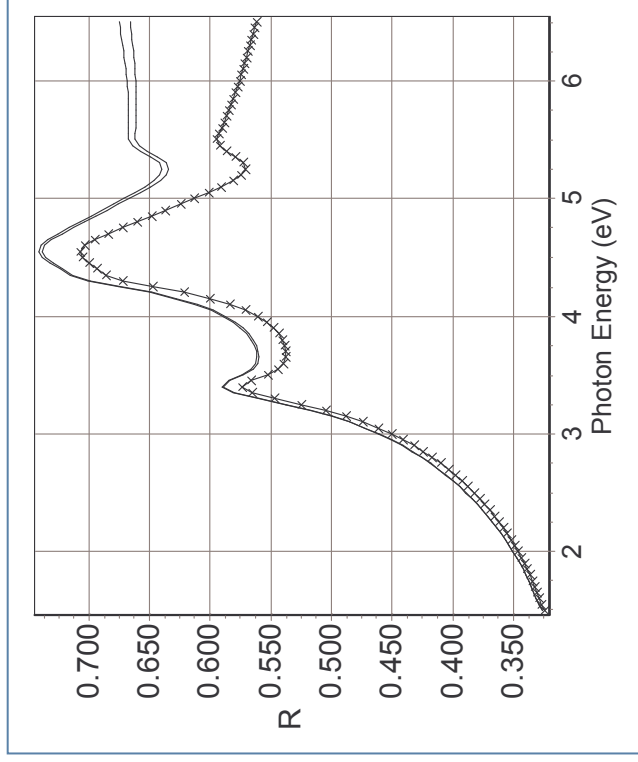
## Advantages

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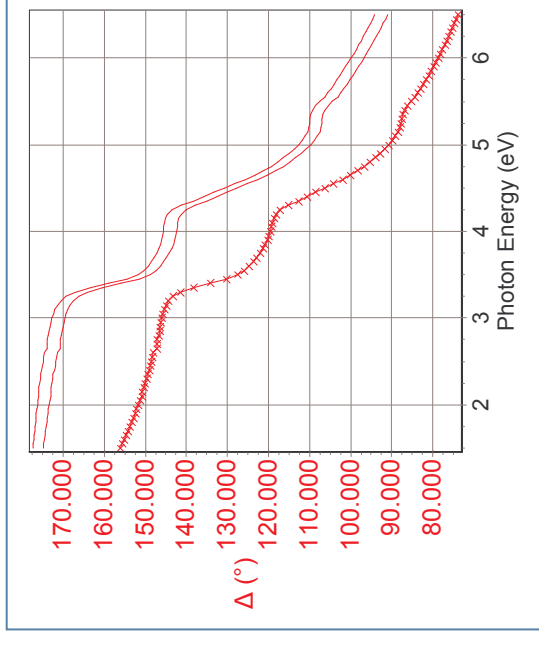
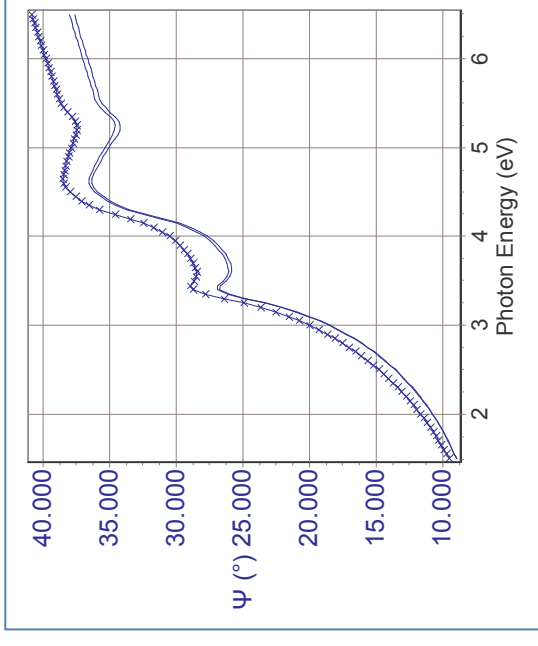
- **Measure ratio of two parameters**
    - Repeatable & accurate
    - No reference necessary
    - Reduced problems of source fluctuation
  - **Measure a phase  $\Delta$** 
    - Very sensitive to film thickness (<10 nm)
  - **Spectroscopic Ellipsometry**
    - Allows multiple film parameter characterization
    - Eliminates period problem for thick films
    - Measures data at wavelength of interest
- ↳ Ellipsometry vs Reflectivity
- ↳ Spectroscopic vs Laser Ellipsometry

# Ellipsometry vs Reflectivity

⇒ Phase ( $\Delta$  parameter) information measured by ellipsometer gives much higher sensitivity to ultra-thin films



— 1 nm  
 - - - 2 nm  
 — x — 10 nm  
 Oxide on c-Si



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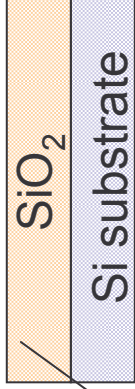
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# Spectroscopic Ellipsometry vs Laser Ellipsometry

⇒ Data cycle as film thickness increases

$$D_{\phi} = \frac{\lambda}{2\sqrt{\tilde{n}_1^2 - \tilde{n}_0^2 \sin^2 \phi}}$$



**Thickness**

500 Å

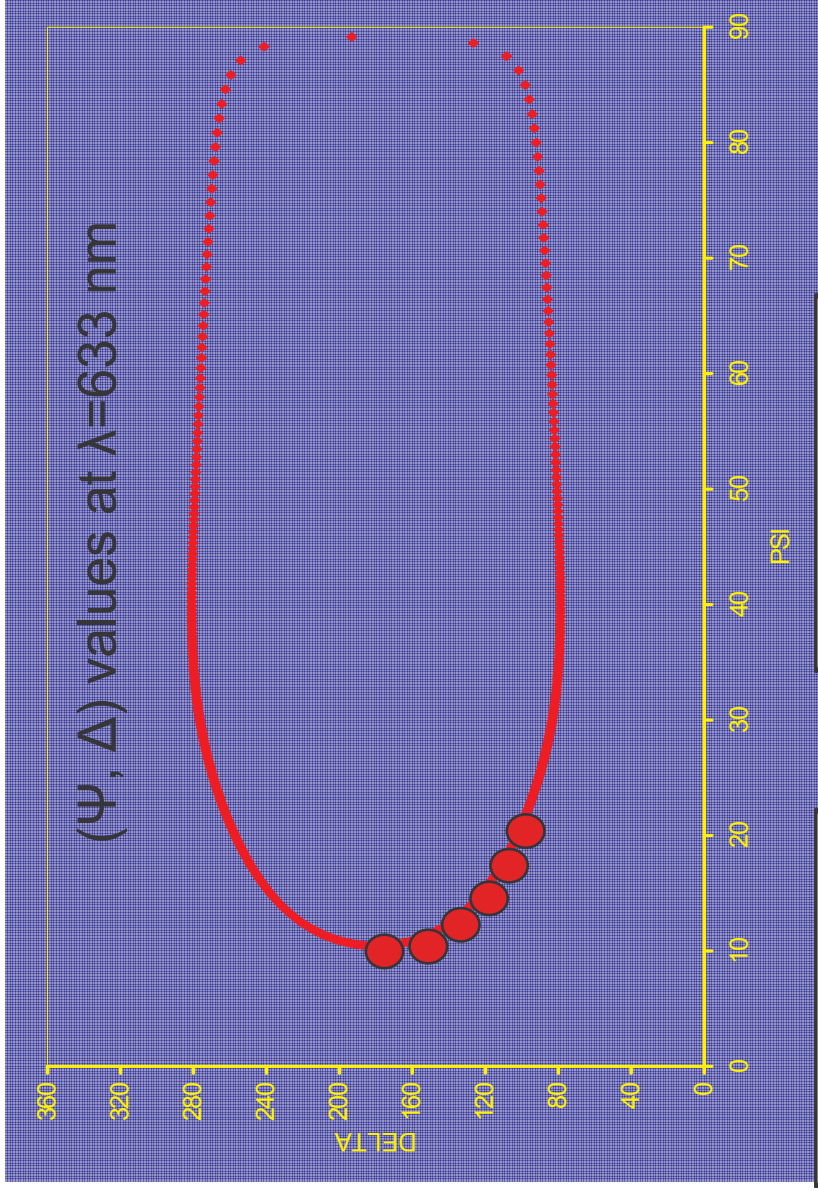
or

3300 Å

or

6100 Å

or.....

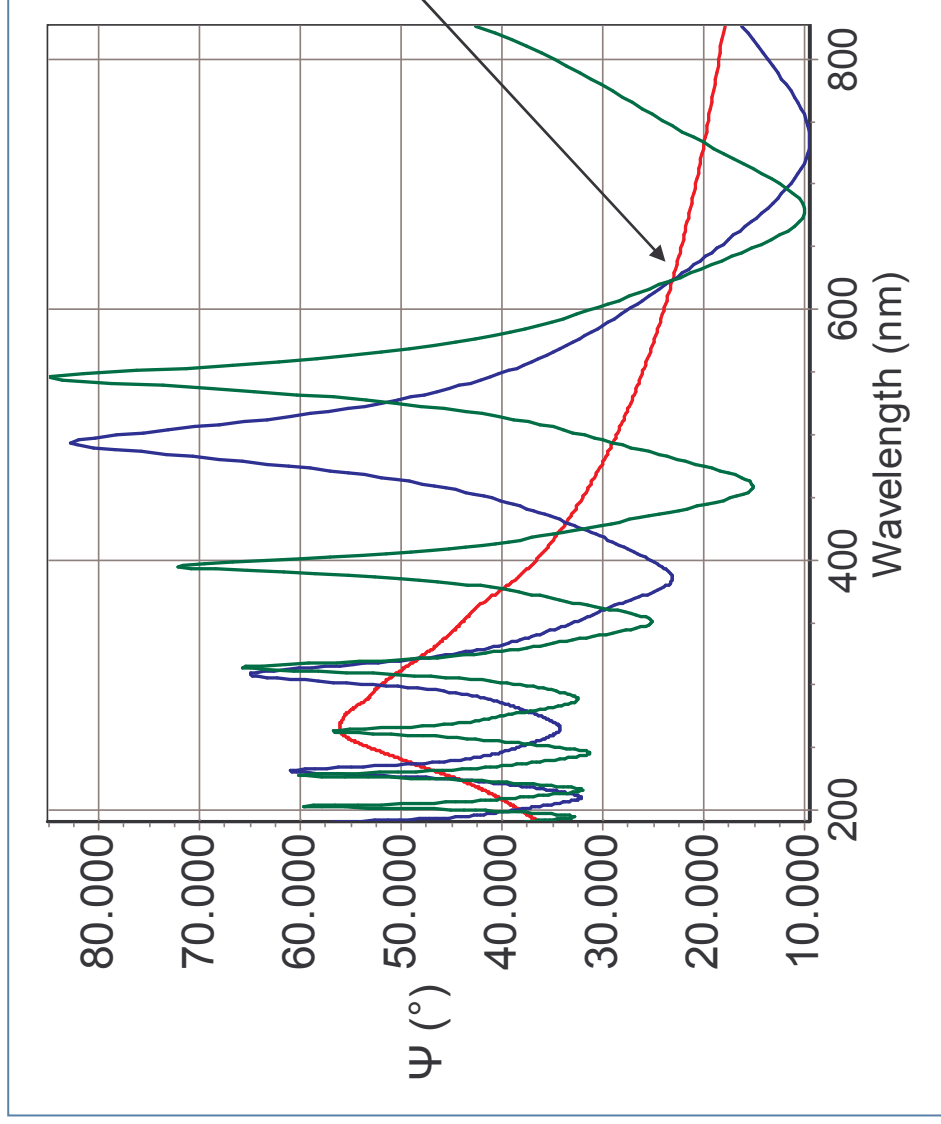


# Spectroscopic Ellipsometry vs Laser Ellipsometry

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- **Vary wavelength**

- Probe different (n,k)
- Thickness constant



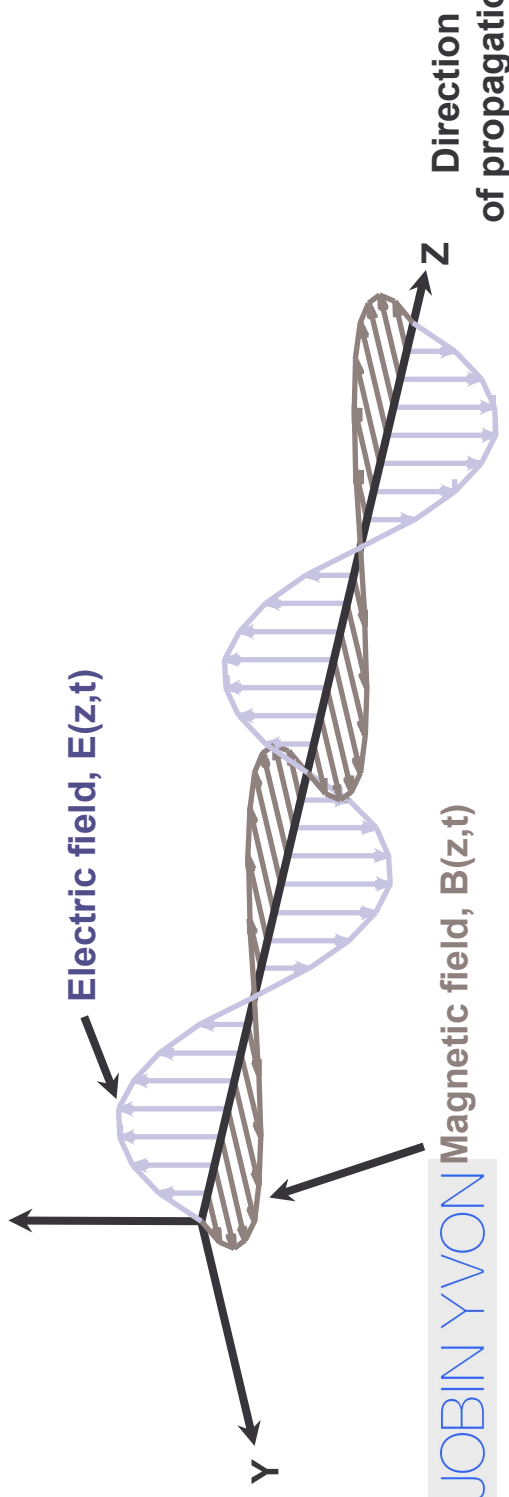
# Interaction of Light with Matter

- **Description of light as an electromagnetic plane wave**
  - Derives from Maxwell's equations
  - Consists of an electric and magnetic field vector oscillating perpendicularly to the direction of propagation

$$E = \text{Re}[E_0 \exp i(\omega t - \mathbf{k} \cdot \mathbf{r} + \phi)]$$

**amplitude**  $2\pi f = \frac{2\pi\lambda}{c}$  **phase**  $\frac{2\pi}{\lambda} z$

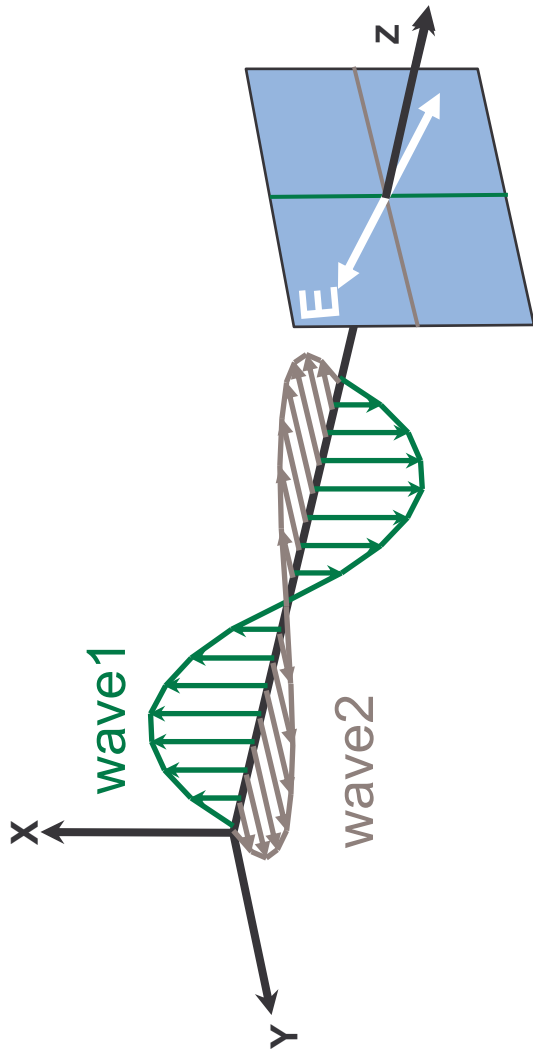
propagation vector



# Light Polarization

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- **Polarization State**
  - Defined by 2 parameters: phase & amplitude of the electric field
  - Describes the direction of the electric field
- **3 Polarization States**
  - Linear polarization
    - > Orthogonal  $E_x$  &  $E_y$  propagating in same direction
    - > Waves are in phase with each others

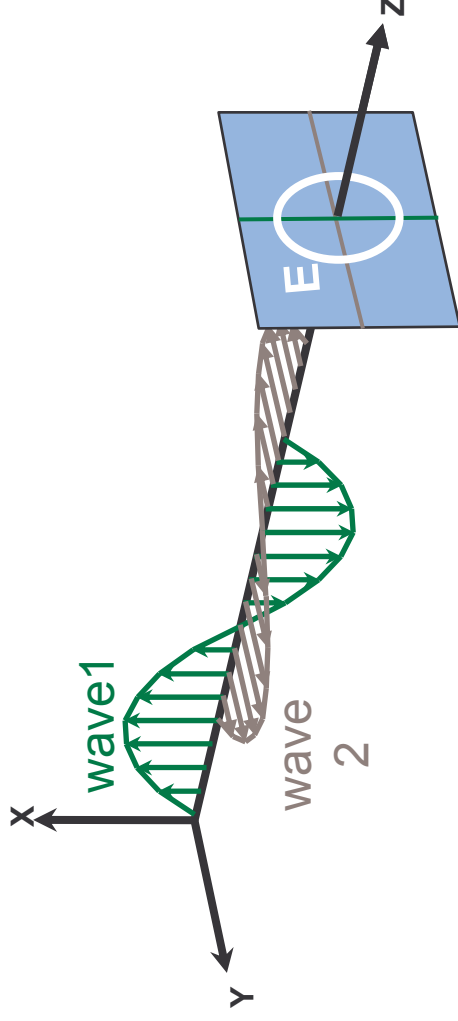




# Light Polarization

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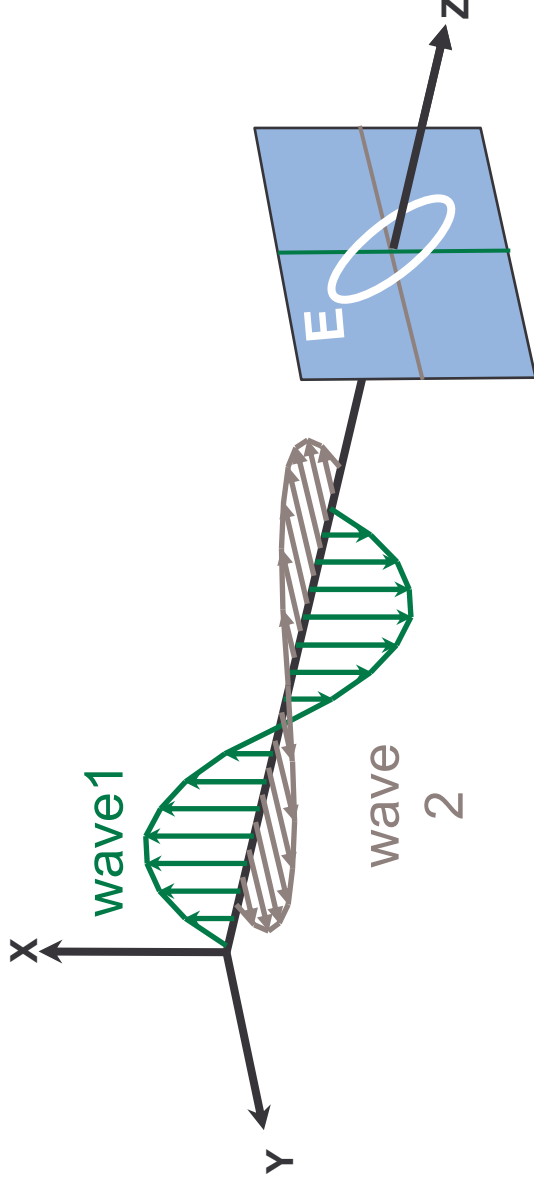
- **3 Polarization States**
  - Circular polarization
    - > Orthogonal  $E_x$  &  $E_y$  are  $90^\circ$  out of phase
    - > Equal amplitude



# Light Polarization

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- **3 Polarization States**
  - Elliptical polarization
    - > Orthogonal  $E_x$  and  $E_y$  have different phase and amplitude



# Electromagnetic Spectrum

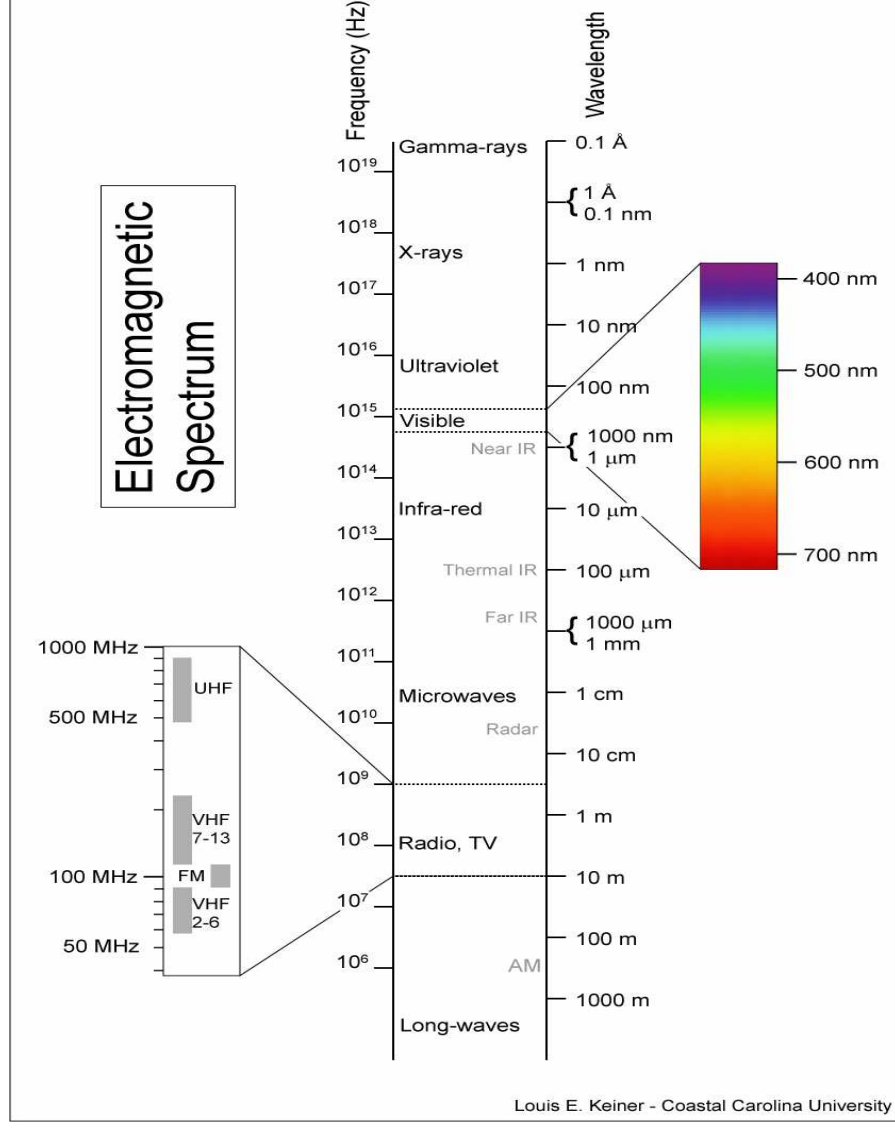
- **Wavelengths units**
  - Wavelength ( $\lambda$ )
  - Photon energy (eV)
  - Wavenumber (K)

- **Relationships**

$$E(\text{eV}) = h\nu = \frac{1240}{\lambda(\text{nm})}$$

$$E(\text{nm}) = E(\text{microns}) \times 1000$$

$$\lambda(\mu\text{m}) = \frac{10000}{K(\text{cm}^{-1})}$$



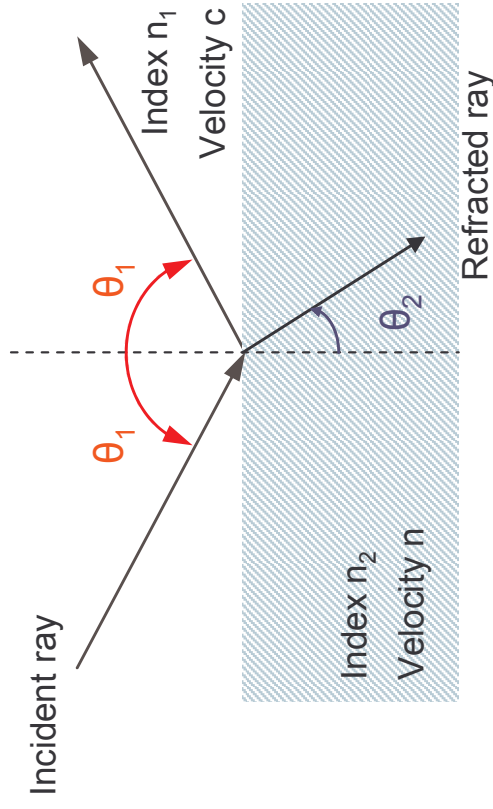
# What are optical constants ?

- 2 parameters used to describe the interaction of light with matter
- Complex Index of refraction :  $\tilde{N} = n - ik$       And  $n^2 - k^2 = \epsilon_1$
- Complex dielectric constant :  $\tilde{\epsilon} = \epsilon_1 - i\epsilon_2$        $2nk = \epsilon_2$
- Ratio of the velocity of light in vacuum ( $c$ ) to its velocity ( $v$ ) in the medium
  - **Refractive index (or index of refraction) :  $n = c/v$**

- Amount of absorption loss when light propagates through the material

- **Extinction coefficient :  $k$**

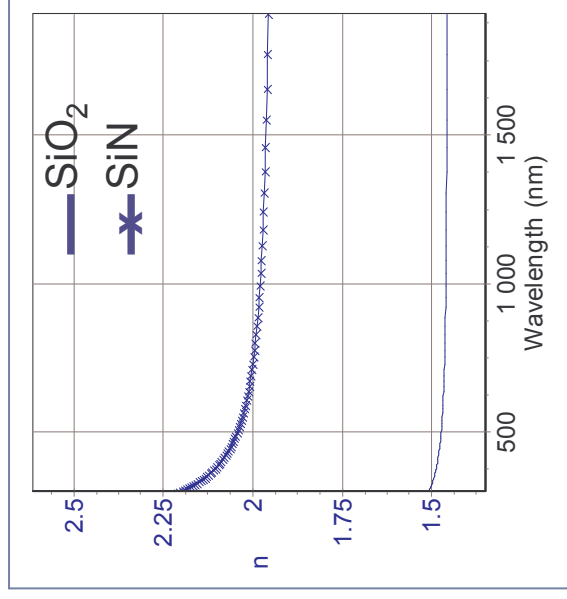
■ Absorption coefficient  $\alpha = \frac{4\pi k}{\lambda}$



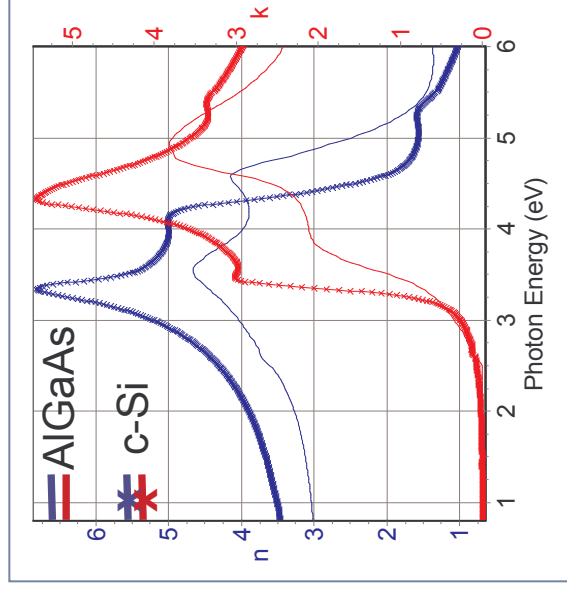
# Optical Constants

- Depend on properties of the material
- Depend on wavelength range measured

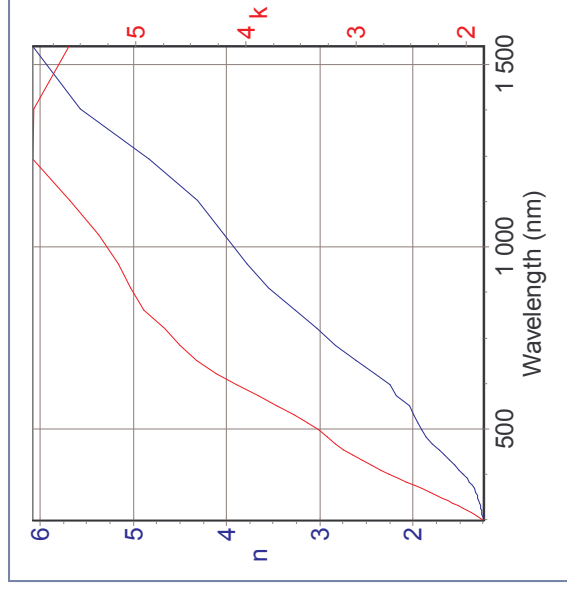
## Dielectric or insulator



## Semiconductor



## Metal



Transparent in the NIR-VIS

Opaque in the VIS

Highly absorbing in the NIR

# Optical Constants

- Representing the  $(n,k)$  of the material in the ellipsometric model

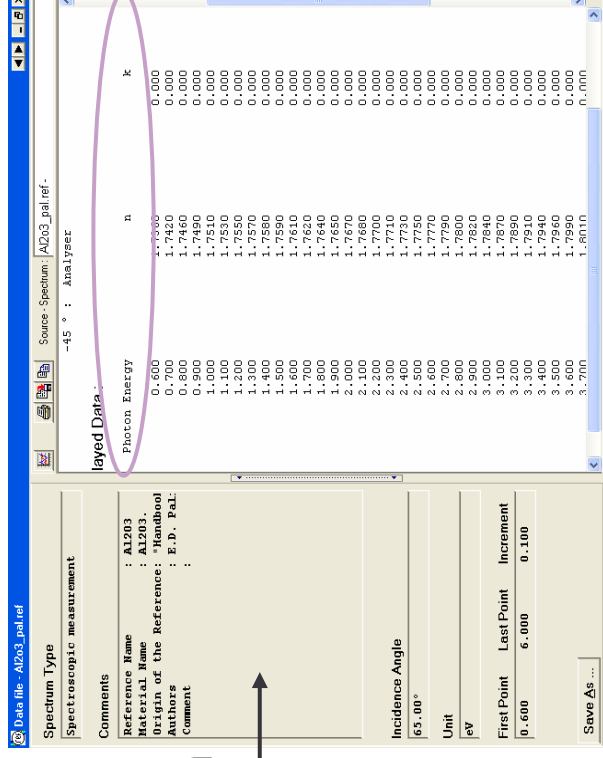
## ⇒ Tabulated references

- No variation, fixed  $(n,k)$  values, often used as a starting values

Library of >100 materials

Ag\_pal.ref  
 A-ga\_as\_isa.ref  
 Age\_asp.ref  
 Al\_as\_isa.ref  
 Al\_asp.ref  
 Al\_IR.ref  
 Al10gaas\_asp.ref  
 Al20gaas\_asp.ref  
 Al2o3\_pal.ref  
 Al2o3\_jy.ref  
 Al2o3-E\_pal.ref  
 Al2o3-E-HT.ref  
 Al2o3-O\_jy.ref  
 Al2o3-O\_pal.ref  
 Al2o3-O-HT.ref  
 Al31gaas\_asp.ref  
 Al42gaas\_asp.ref  
 Al49gaas\_asp.ref  
 Al59gaas\_asp.ref  
 Al70gaas\_asp.ref  
 Al80gaas\_asp.ref

List of  $(n,k)$  values with wavelengths



1 [F] 20.0 Al2o3\_pal.ref X

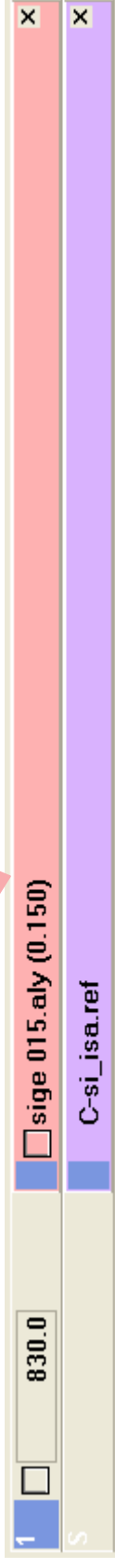
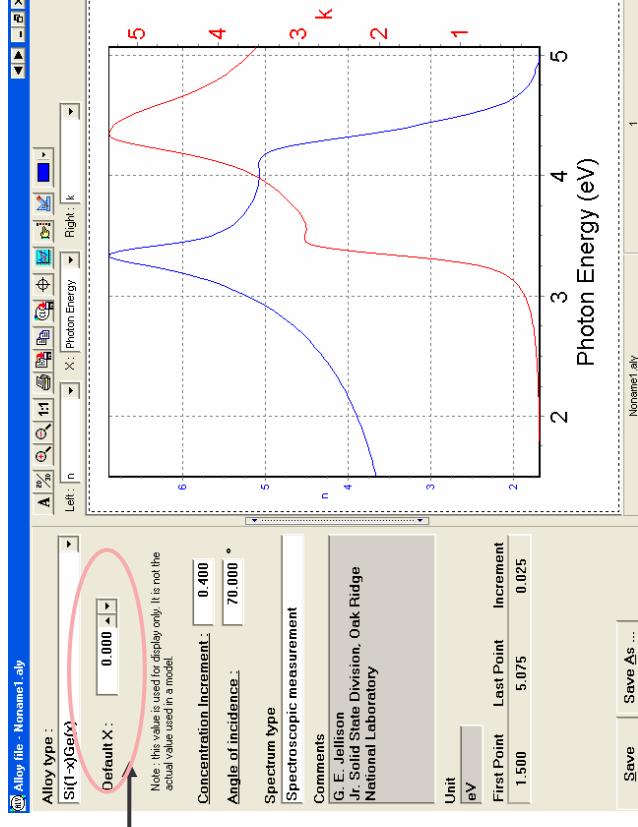
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# Optical Constants

- Representing the  $(n, k)$  of the material in the ellipsometric model
  - ⇒ **Compound alloy semiconductor references**
    - Known variation

Adjust the composition and generate the  $(n, k)$

Library of 5 semiconductor alloys



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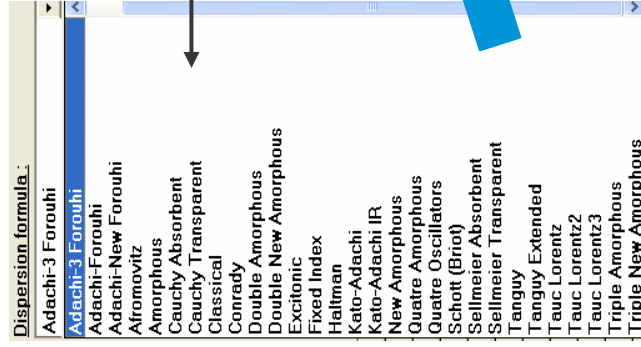
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# Optical Constants

- Representing the  $(n, k)$  of the material in the ellipsometric model

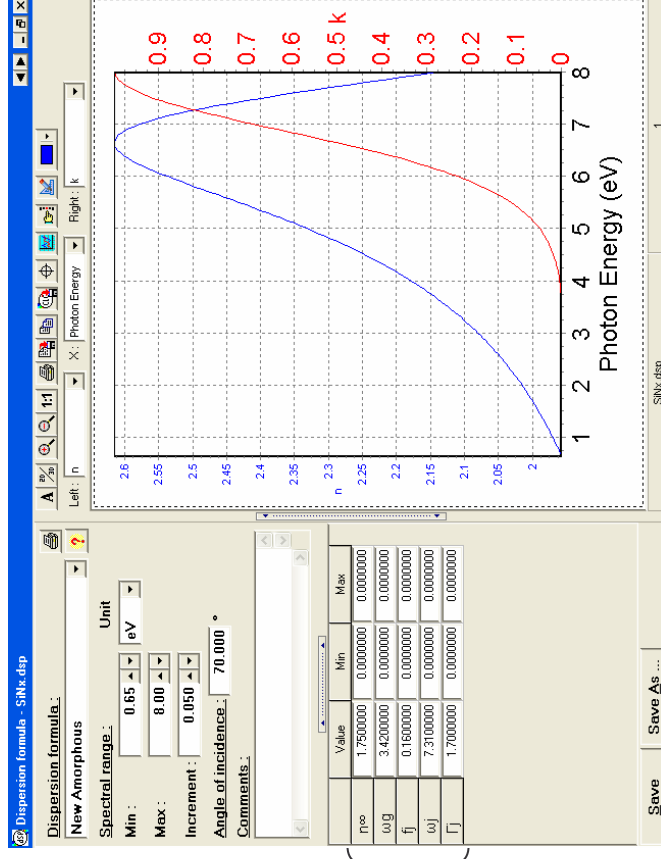
⇒ **Dispersion relationships**

– Build « by yourself » the  $(n, k)$  of your material



Library of > 30 dispersion formula

Setting values of parameters describing the dispersion formula



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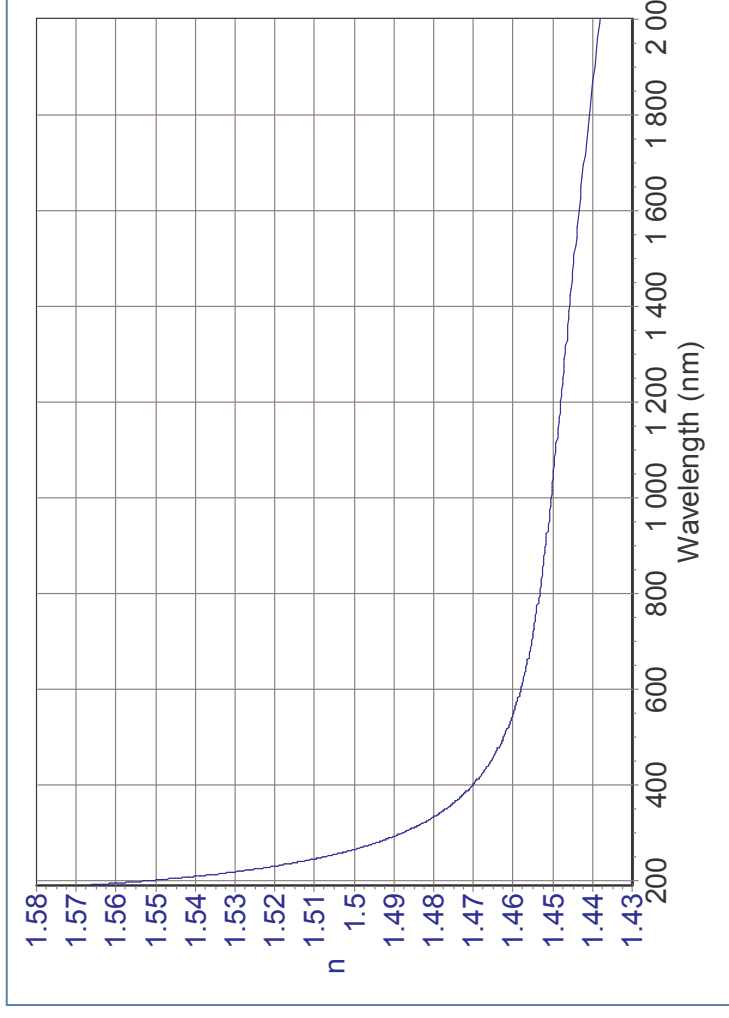


# Material Dispersion in Optics

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- Materials dispersion comes from a wavelength dependant response of a material to waves.

⇒ Optical constants vary with wavelength, it is called a dispersion.

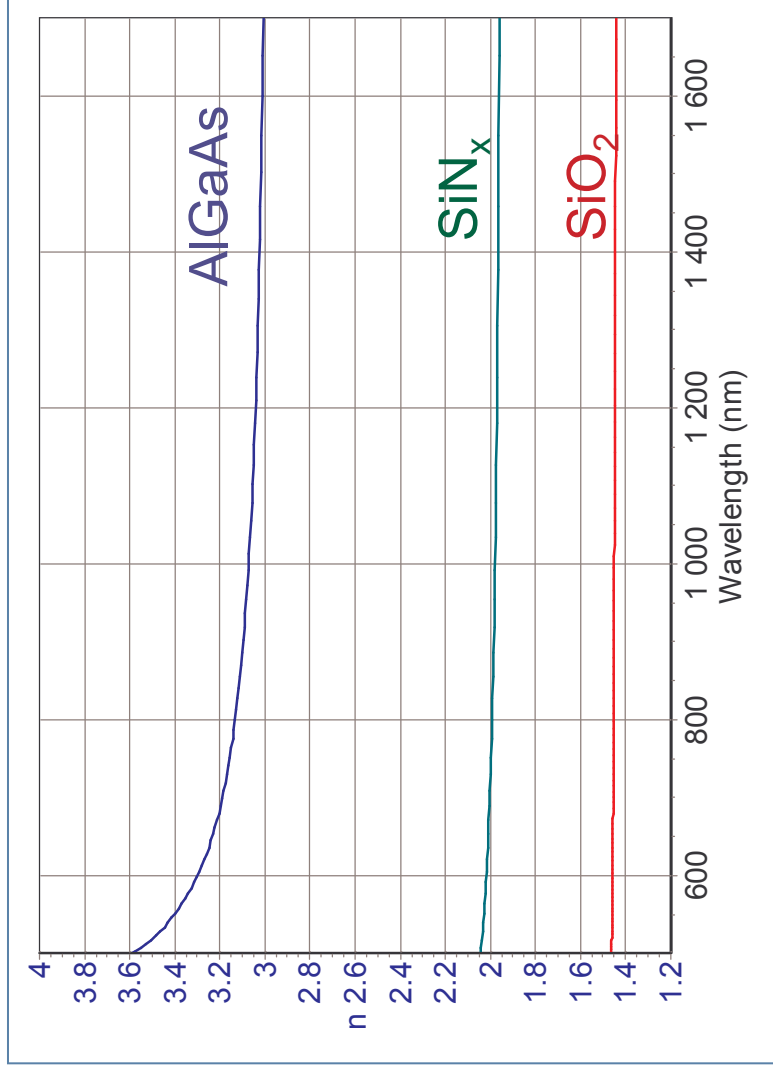


## Normal Dispersion: Transparent Material

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- Refractive index decreases with increasing wavelength  $\lambda$
- No absorption ( $k=0$ ): transparent material
- Higher index for stronger UV absorption

⇒ Normal dispersion

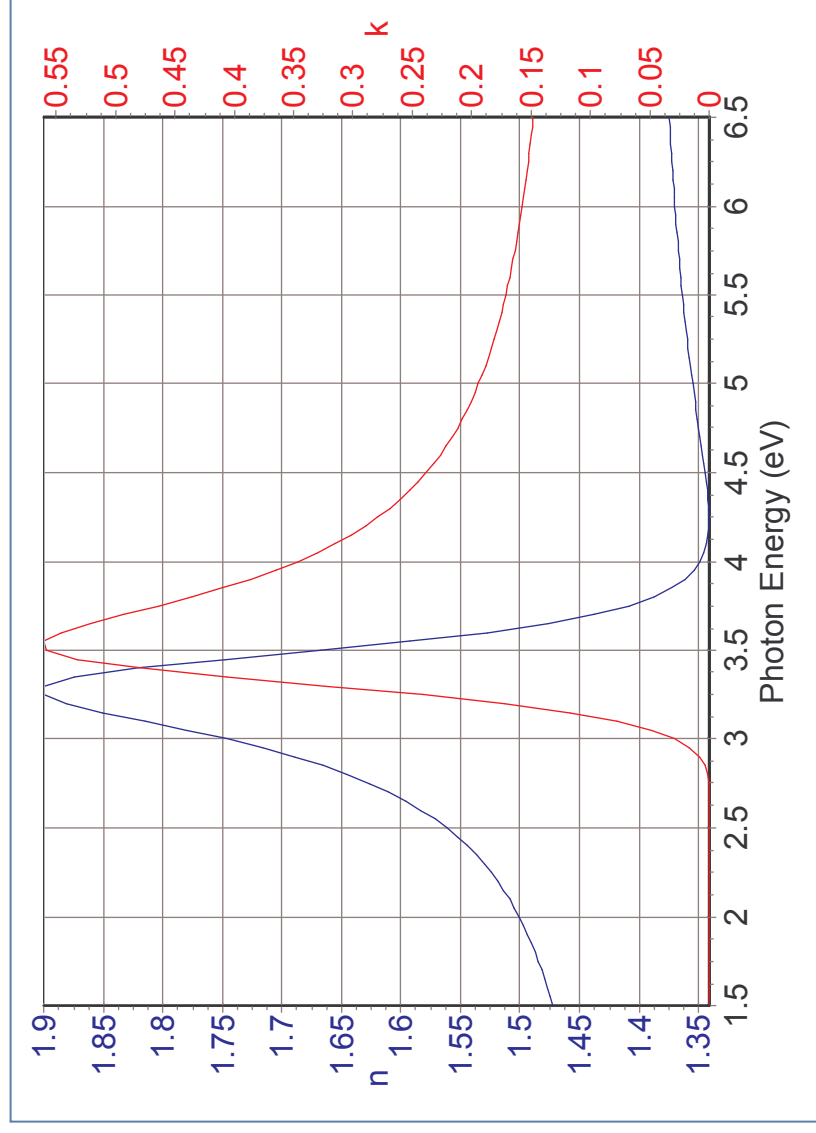


# Anomalous Dispersion: Absorbing Material

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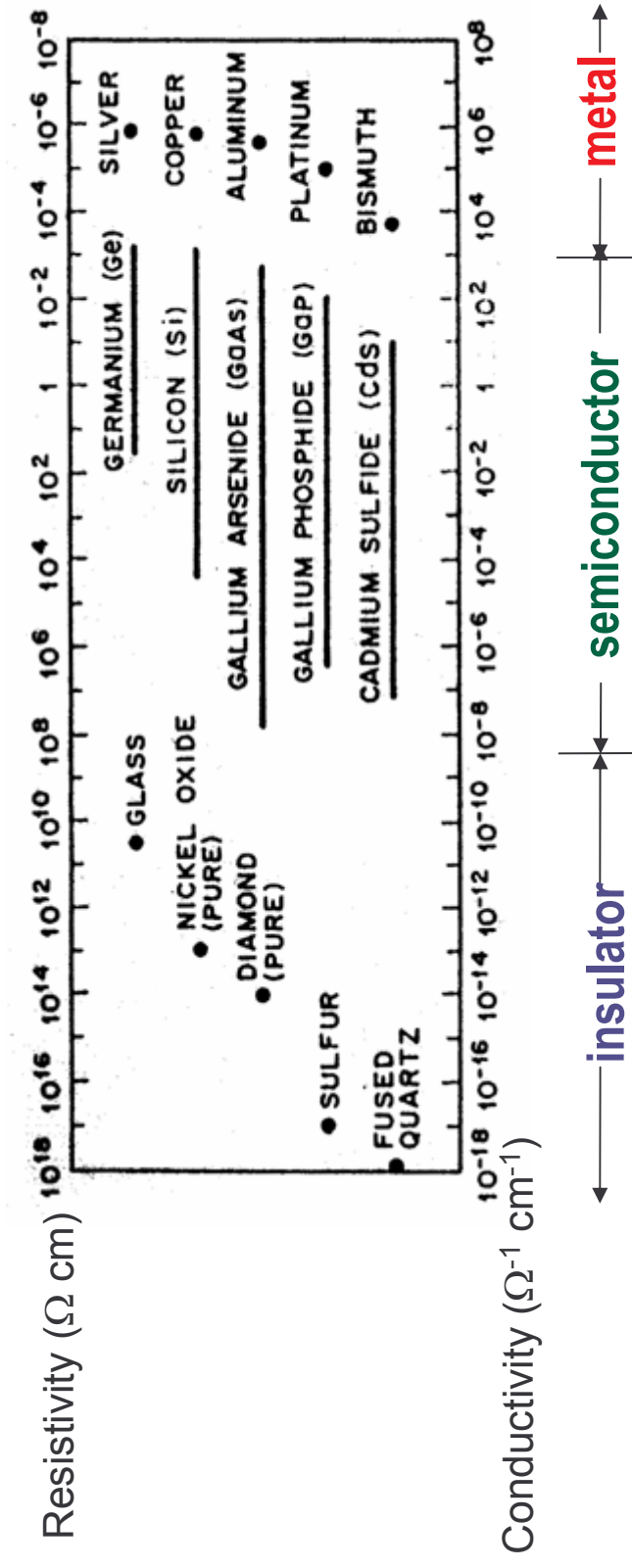
- Refractive index increases with increasing wavelength  $\lambda$
- Absorption ( $k \neq 0$ ): absorbing material
- Higher index for stronger UV absorption

⇒ Anomalous dispersion



# Classes of Materials

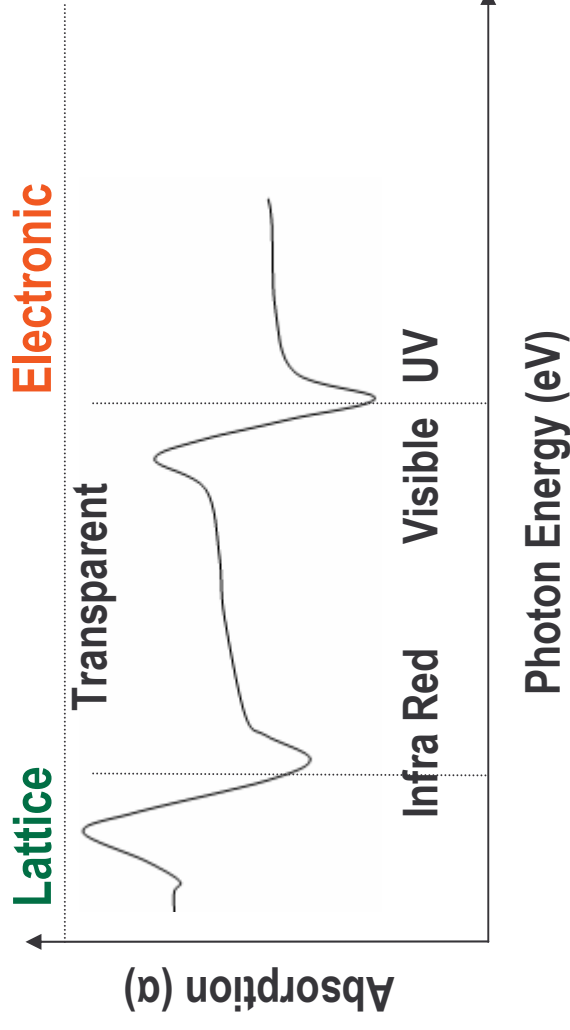
- Classified versus electrical conductivity
  - **Metal**: no gap  $E_g = 0$
  - **Insulator** (dielectric): large gap  $E_g > 4 \text{ eV}$
  - **Semiconductor**:  $0 < E_g < 4 \text{ eV}$



# Material Absorption Theory

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- 3 fundamental processes involving interaction between material and EM wave
  - Electronic absorption
  - Lattice or phonon absorption
  - Free carrier absorption

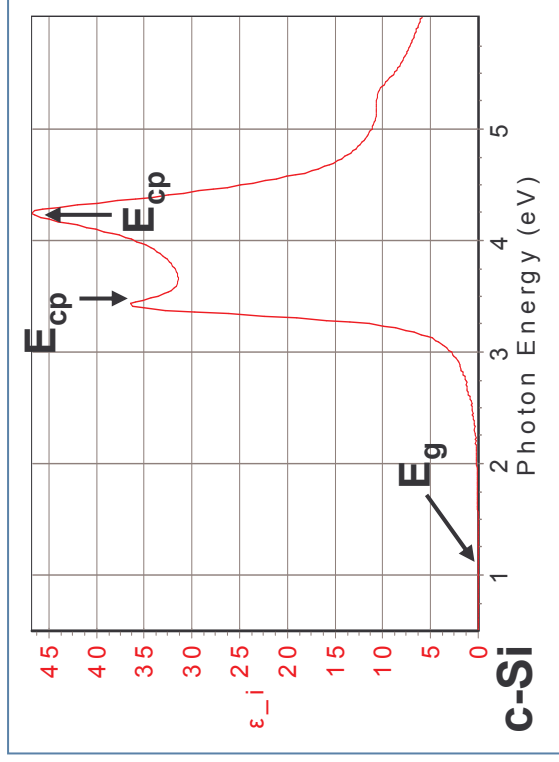
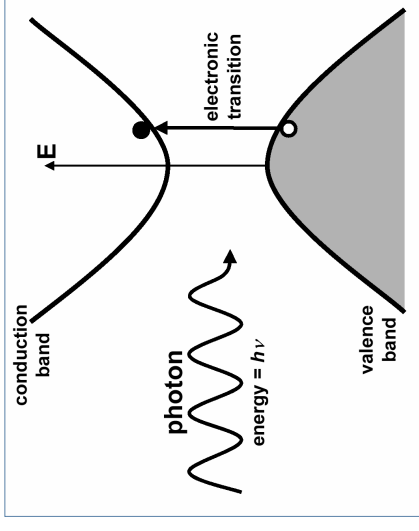


# Absorbing Regions

## Electronic transitions

■ Result of interaction between the incident light and the motions of e<sup>-</sup> or holes within the material

- Electrons in valence band
- Gap between valence & conduction band
- If photon has energy larger than gap, electron may excite to higher state



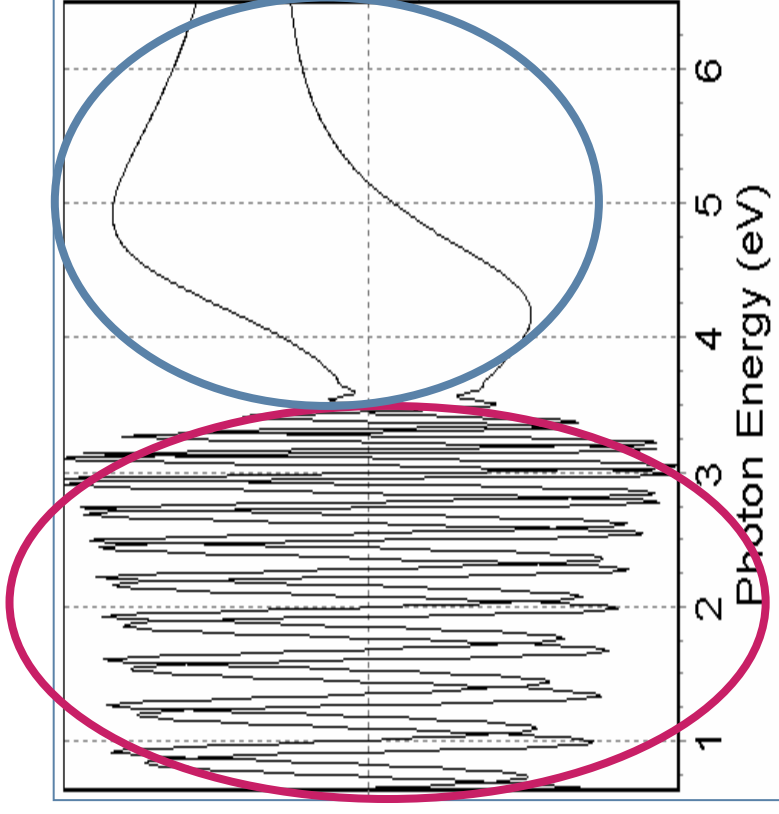
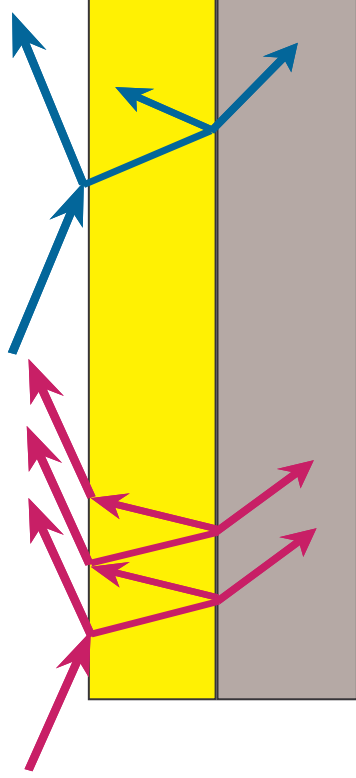
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- Absorption associated with each transition
- Band-gap energy ( $E_g$ ): minimum energy where transitions can occur
- Critical point energies ( $E_{cp}$ ) = photon energies where there is a high probability of band-to-band transitions

## Reflections with Films

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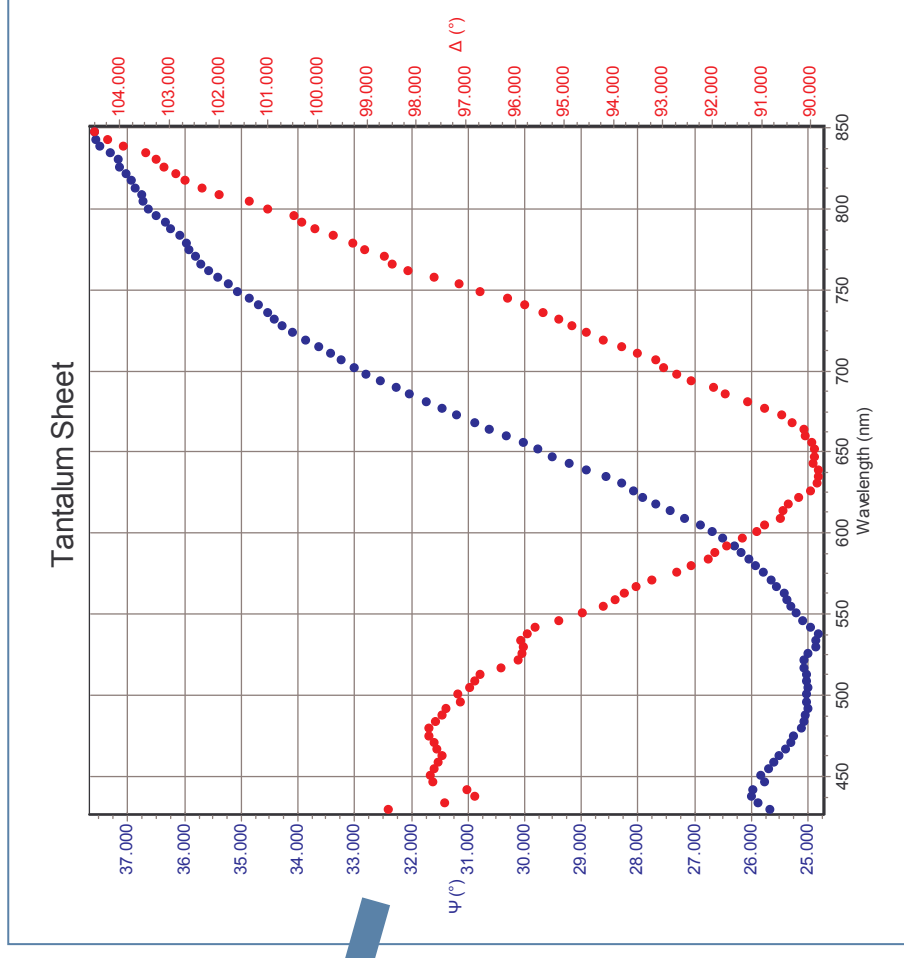
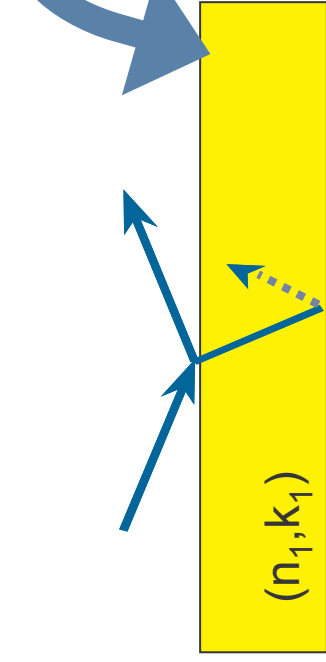
- **Transparent film:** see interference fringes ( $>1000 \text{ \AA}$ )
  - ⇒ Thicker films produces more interference fringes (in the example  $\text{TiO}_2$  layer thickness:  $8000 \text{ \AA}$ )
- **Absorbing film:** no interference fringes, behaves as a substrate



# Bulk Sample or Substrate

- Measurement of a bulk sample gives directly the  $(n, k)$  of the material

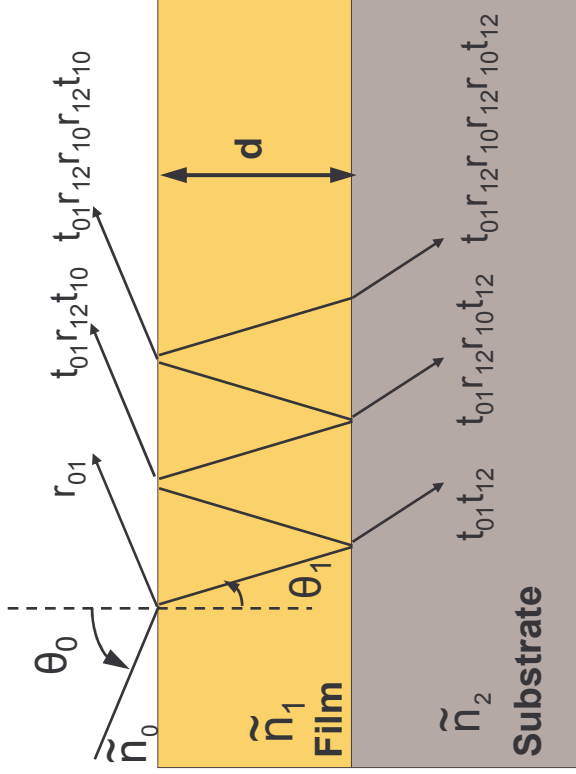
- Ratio  $\rho \Rightarrow (\Psi, \Delta) = f(\varepsilon_0, \varepsilon_1, \theta_0)$
- 2 measured parameters :  $(\Psi, \Delta)$
- 2 unknowns :  $n_1, k_1$





# Thin Film on Substrate

- Thin film characterization: thickness and  $(n, k)$



$R = \Sigma r$  related to the 1&2 interfaces

$$R = \frac{r_{01} + r_{12} e^{-2j\beta}}{1 + r_{01} r_{12} e^{-2j\beta}}$$

$\beta$  : Film phase thickness

$$\beta = 2\pi \left( \frac{d}{\lambda} \right) n_1 \cos \phi_1$$

Ratio  $\rho \Rightarrow (\Psi, \Delta) = f(\varepsilon_0, \varepsilon_1, \varepsilon_2, \theta_0, d, \lambda_0)$

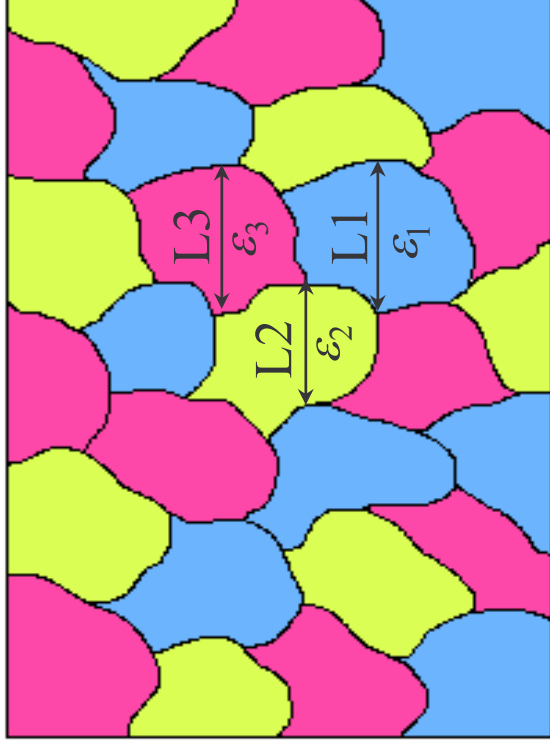
2 measured parameters :  $(\Psi, \Delta)$

3 unknowns :  $n_1, k_1$  and  $d$

# Effective Medium Approximation Theory

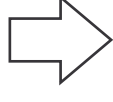
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- All materials are inhomogeneous on atomic scale
- Part of macroscopically homogeneous materials is inhomogeneous on microscopic scale



If each separate region is large enough to possess their own dielectric identities, but small compared to wavelength of light

$$(L_1, L_2, L_3 < \lambda)$$



*Effective Medium Approximation*  
can be used

- EMA is used to calculate the dielectric functions of mixed phases based on their microstructure and component volume fractions

# Effective Medium Approximation (EMA)

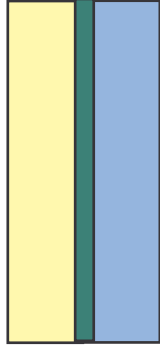
⇒ Calculate optical constants of mixed materials (handled by the software !)

Surface roughness



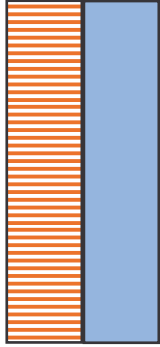
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1	<input type="checkbox"/> F	1148.0		<input type="checkbox"/> F	SiNx.dsp					<input checked="" type="checkbox"/> X
2					Csi_wor.ref					<input checked="" type="checkbox"/> X

Interface



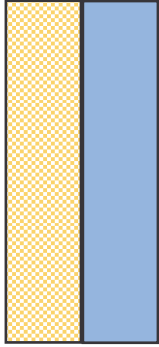
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4	<input type="checkbox"/> F	100.0	<input type="checkbox"/> %	<input type="checkbox"/> F	P-st-as_jel.ref	50.00 %	<input checked="" type="checkbox"/> X	<input type="checkbox"/> F	SiO2_cl.dsp	50.00 %	<input checked="" type="checkbox"/> X
3	<input type="checkbox"/> F	4000.0		<input type="checkbox"/> F	P-st-as_jel.ref					<input checked="" type="checkbox"/> X	
2	<input type="checkbox"/>	790.0		<input type="checkbox"/>	sin_new_tl_wd.dsp					<input checked="" type="checkbox"/> X	
1	<input type="checkbox"/>	1807.0		<input type="checkbox"/>	SiO2_isa.ref					<input checked="" type="checkbox"/> X	
5					C-st_isa.ref					<input checked="" type="checkbox"/> X	

Porosity



3	<input type="checkbox"/> F	350.0	<input type="checkbox"/> %	<input type="checkbox"/>	Csi_wor.ref	45.00 %	<input checked="" type="checkbox"/> X	SiO2_isare	35.00 %	<input checked="" type="checkbox"/> X	Void.ref	20.00 %	<input checked="" type="checkbox"/> X
2	<input type="checkbox"/> F	500.0	<input type="checkbox"/> %	<input type="checkbox"/>	Csi_wor.ref	64.00 %	<input checked="" type="checkbox"/> X	SiO2_isare	25.00 %	<input checked="" type="checkbox"/> X	Void.ref	11.00 %	<input checked="" type="checkbox"/> X
1	<input type="checkbox"/>	1500.0	<input type="checkbox"/> %	<input type="checkbox"/>	Csi_wor.ref	82.00 %	<input checked="" type="checkbox"/> X	SiO2_isare	11.00 %	<input checked="" type="checkbox"/> X	Void.ref	7.00 %	<input checked="" type="checkbox"/> X
5					Csi_wor.ref								<input checked="" type="checkbox"/> X

Polycrystalline materials



2	<input type="checkbox"/> F	1963.2	<input type="checkbox"/> %	<input type="checkbox"/>	Asi_asp.ref	20.00 %	<input checked="" type="checkbox"/> X	Csi_wor.ref	80.00 %	<input checked="" type="checkbox"/> X
1	<input type="checkbox"/>	5000000.0		<input type="checkbox"/>	glassnew.dsp					<input checked="" type="checkbox"/> X
5					void.dsp					<input checked="" type="checkbox"/> X

# Effective Medium Theory

## Maxwell Garnett and Bruggeman models

---

### ▪ Maxwell Garnett model

- The Maxwell-Garnett is derived assuming spherical inclusions (denoted  $\epsilon_i$ ) with a volume fractions  $f$  exist in a host matrix of the second material (denoted  $\epsilon_h$ )

$$\epsilon = \epsilon_h \frac{\epsilon_i(1+2f) + 2\epsilon_h(1-f)}{\epsilon_i(1-f) + \epsilon_h(2+f)}$$

### ▪ Bruggeman model

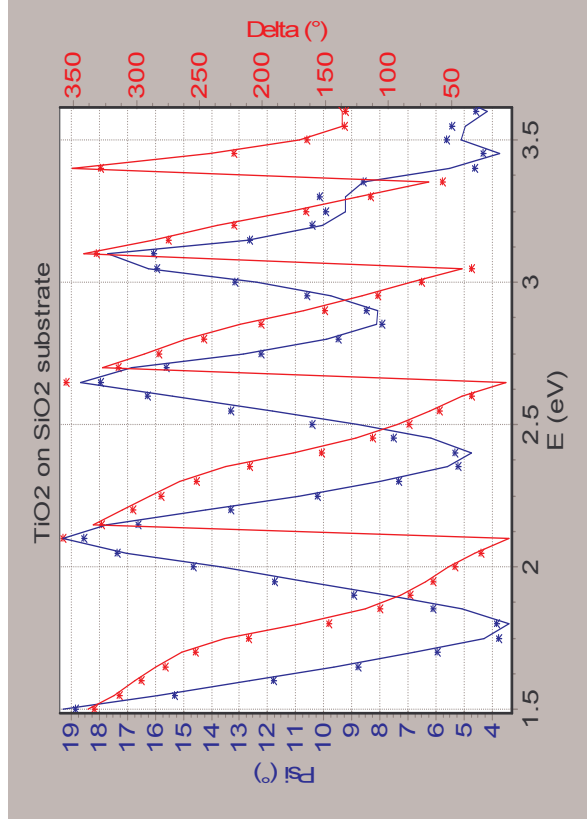
- Non restrictive of the number of components of the mixture which are treated in an equivalent way by holding account only of their proportion
- Self-consistent theory: Host material complex dielectric function equalling the final effective complex dielectric function of the multi-constituent material

$$\sum_i f_i \frac{\epsilon_i - \epsilon}{\epsilon_i + 2\epsilon}$$

# ANALYSIS OF ELLIPSOMETRIC DATA

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- Ellipsometry does not measure film thicknesses or optical constants, it measures  $\Psi$  and  $\Delta$



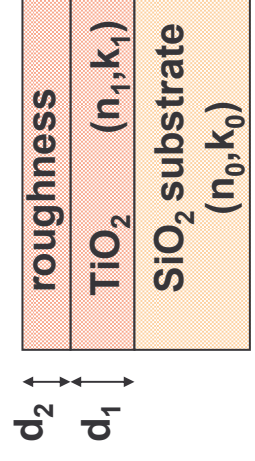
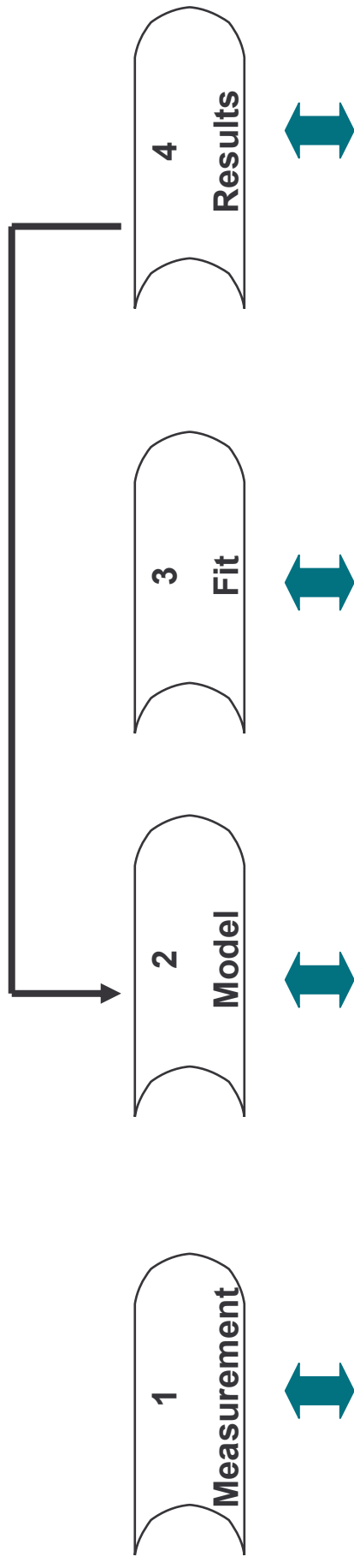
- To extract these informations from a sample, it is necessary to perform a **model dependant analysis** of the ellipsometric angles
- A model is an idealized mathematical representation of the sample

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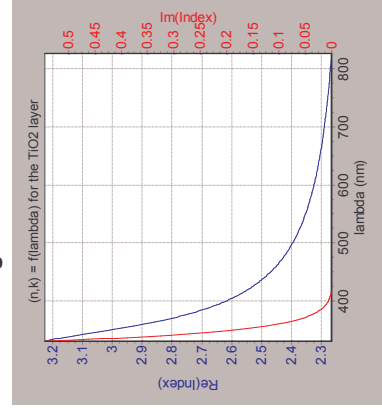
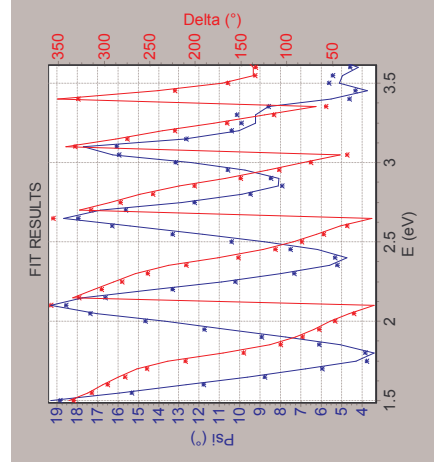
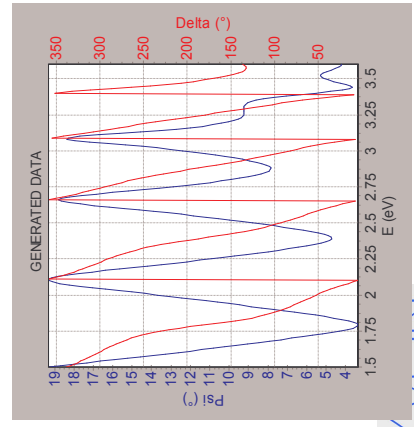
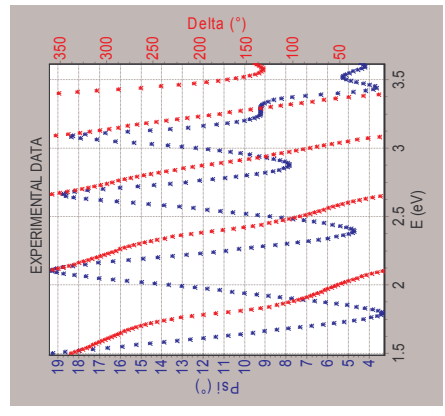
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# SPECTROSCOPIC ELLIPSOMETRY DATA ANALYSIS FLOWCHART



$$\left\{ \begin{array}{l} \chi^2 = 2.1 \rightarrow \chi^2 = 1.6 \\ d_{\text{TiO}_2} = 4200 \text{ \AA} \\ d_{\text{rough}} = 20 \text{ \AA} \end{array} \right.$$



## Data Fitting

$$\chi^2 = \min \sum_{i=1}^n \left[ \frac{(\Psi_{\text{th}} - \Psi_{\text{exp}})_i^2}{\Gamma_{\Psi,i}} + \frac{(\Delta_{\text{th}} - \Delta_{\text{exp}})_i^2}{\Gamma_{\Delta,i}} \right]$$

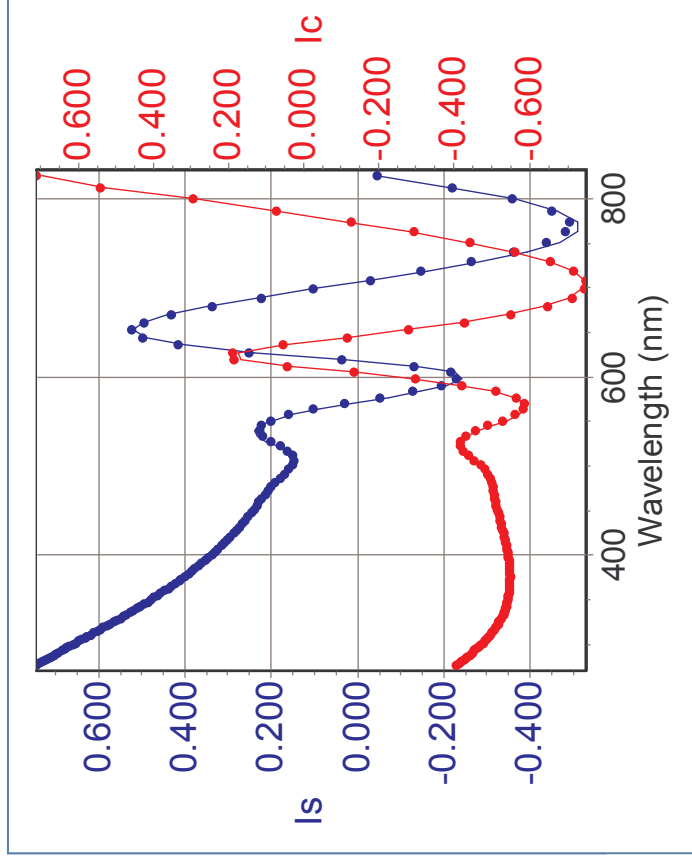
- $\chi^2$  parameter quantifies the difference between experimental and model data
- Software adjusts fit parameters to find best match between model and experimental curves

<b>Roughness</b>
<b>a-Si</b>
<b>Glass substrate</b>

**23 Å**  
**2396 Å**

**Results  $X^2 = 7.8 \rightarrow X^2 = 0.5$**

- A smaller  $\chi^2$  implies a better fit



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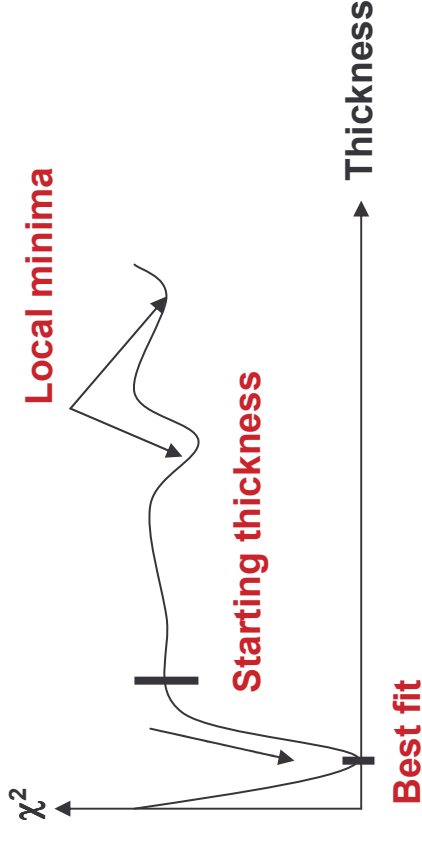
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# Data Fitting

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- **Minimization methods**
  - Levenberg-Marquardt algorithm : commonly used
  - Others: Simplex, ...
- **Difficulties**
  - Local minimum
  - Many variables
  - Setting starting parameters: have to be close to the final solution
- **Getting good starting values**
  - ① Use the simulation function
    - Generate from model and compare with experimental data



- ② Fit the selected parameters

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# Evaluate the Quality of Results

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- Compare experimental data with generated data
- How low is the  $\chi^2$  ? Can it be reduced further by increasing model complexity ?
- Are fit parameters physical ?
- Check the correlation matrix. Values close to 1 mean correlated parameters, and a non-unique solution.

## Correlation matrix $\Leftrightarrow$ 6 fit parameters

=1=	=2=	=3=	=4=	=5=	=6=
1.000	-0.431	-0.148	-0.012	-0.225	0.115
	1.000	0.475	0.127	-0.746	-0.014
		1.000	0.890	-0.474	0.765
			1.000	-0.205	0.970
				1.000	-0.123
					1.000

# General Rules for Ellipsometric Data Analysis

---

## 3 essential steps

### 1 - Experimental measurement

- Check the good working of the ellipsometer (NIST)
- Sample preparation
- Acquisition parameter choices
  - Spectral range (NIR-FUV) / sample properties
  - Monochromator step / layer thickness
  - Angle of incidence (brewster)
  - Beam diameter

# General Rules for Ellipsometric Data Analysis

---

## 3 essential steps

### 2 - Modeling

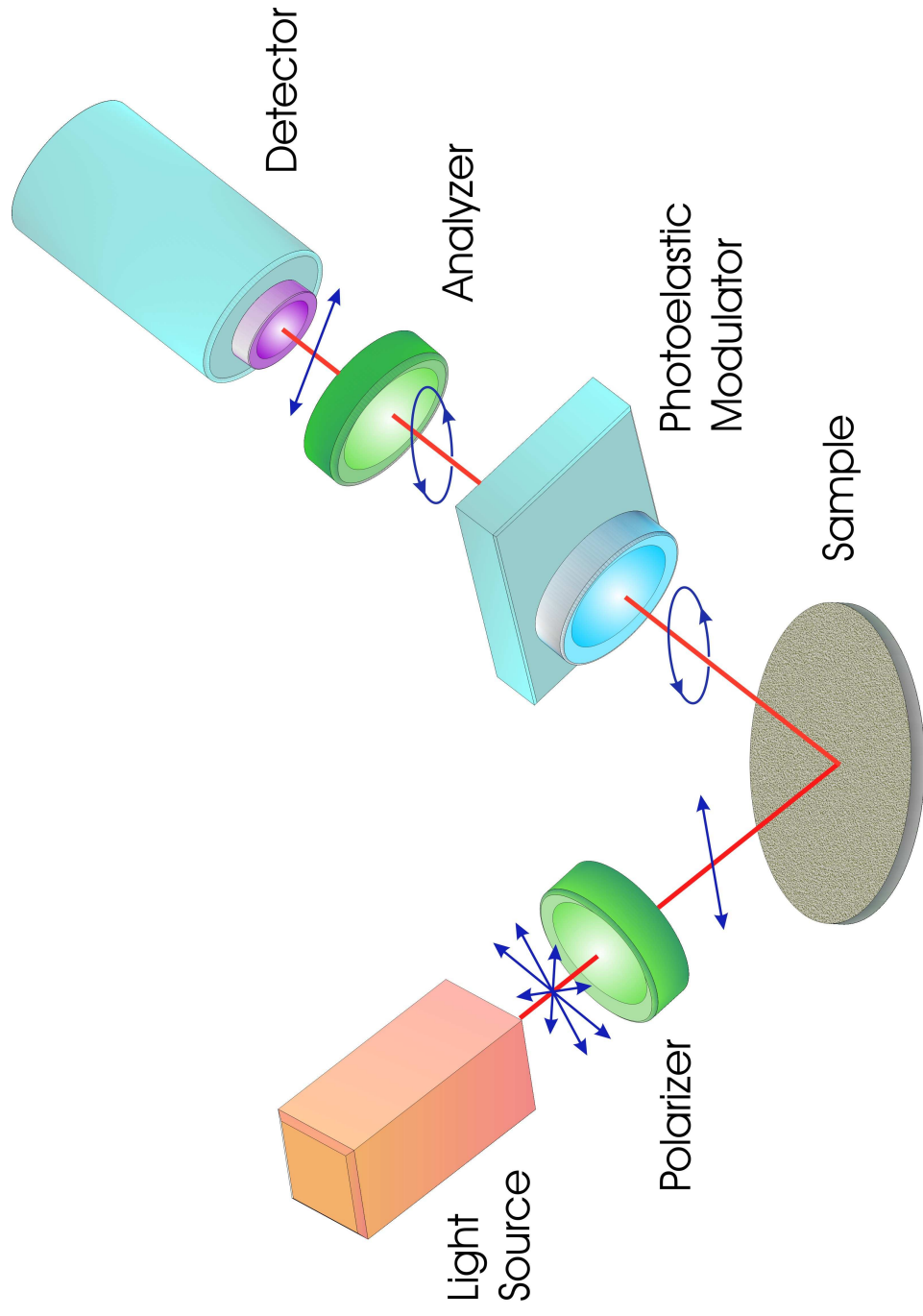
→ Build the most realistic optical model

### 3 - Reliable model choice

- Criteria and quality of a good fit
- Physical result (model and parameter values)
  - Slight correlation between parameters : uniqueness of the solution
  - Final result independent of initial parameters
  - Quick convergence

# Phase Modulation Spectroscopic Ellipsometer

## Optical Set-up



**UVISEL**

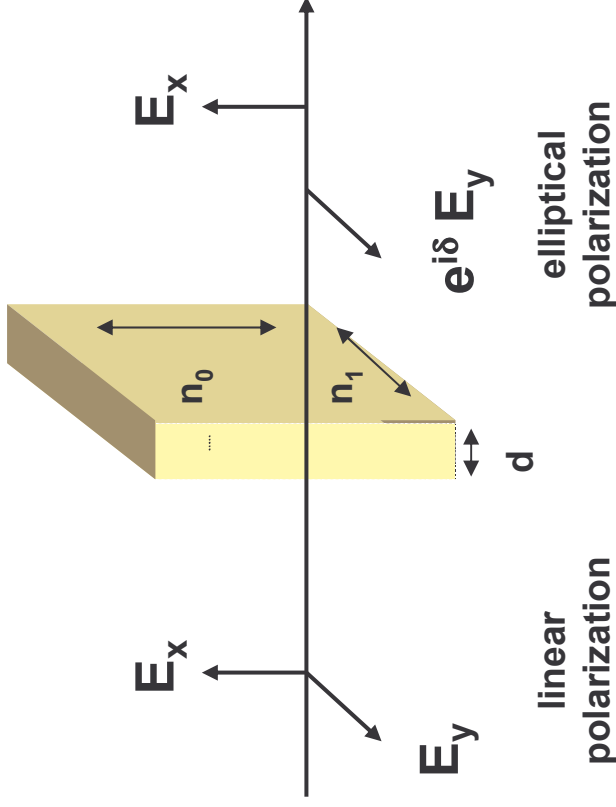
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# What is a photoelastic modulator and How does it work ?

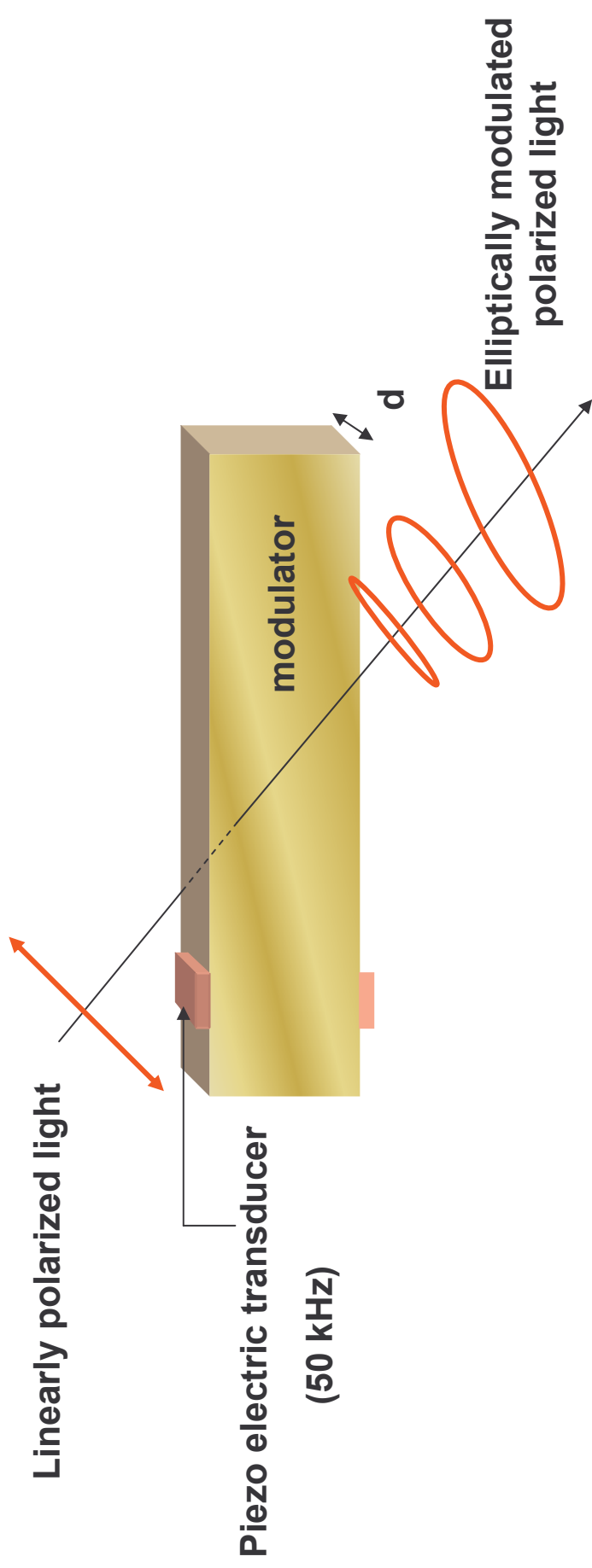
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- **PEM definition**
    - fused silica bar sandwiched between piezo oscillating at the frequency  $w=50 \text{ kHz}$
  - **Stress effect**
    - creation of an optical anisotropy in the silica bar
  - **Strain modulation**
    - optical anisotropy modulated
    - polarization modulated
  - **Modulated phase shift  $\delta(t)$** 
    - $$\delta(t) = A \sin \omega t$$
- with :  $A = 2\pi d (N_1 - N_0) / \lambda$

# What is a photoelastic modulator and How does it work ?

---



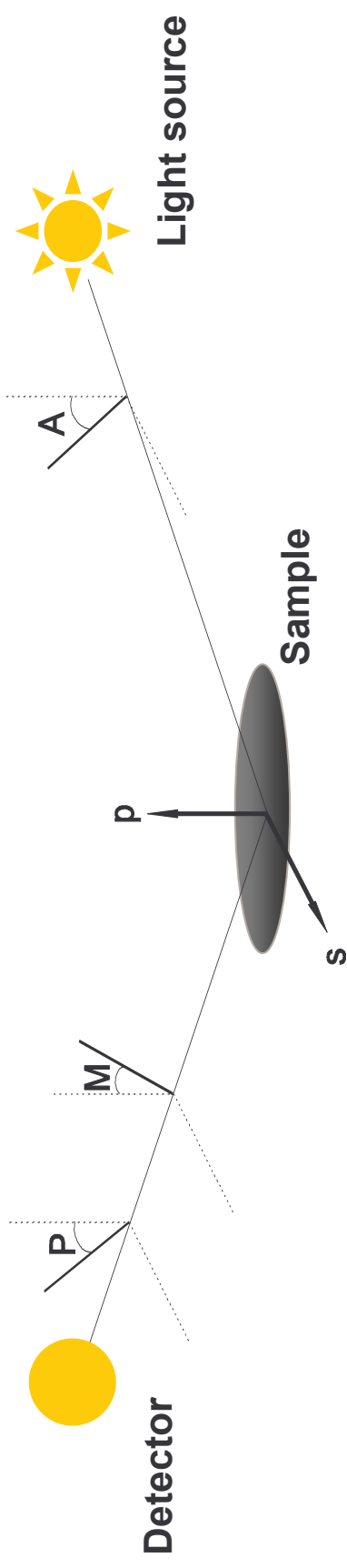
# Phase Modulation Formalism

Based on Jones Formalism

---

- Reference basis  $(\vec{p}, \vec{s})$
- Each element of the optical chain is associated to a matrix (2x2)
  - Sample  $E = \begin{pmatrix} r_p & 0 \\ 0 & r_s \end{pmatrix}$
  - Polarizer  $P = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}$
  - Modulator  $M = \begin{pmatrix} e^{i\delta} & 0 \\ 0 & 1 \end{pmatrix}$
- Coordinate system rotation  $R(\theta) = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix}$

# Phase Modulation Formalism



- Jones formalism for transmitted field :  $E_t = T(A) R_A S R_M M R_{P-M} P E_i$  (I)

- Leading to detected intensity :  $I(t) = E_t E_t^* = I [I_0 + I_S \sin \delta(t) + I_C \cos \delta(t)]$

- Development of equation (I) leads to :

$$I_0 = 1 - \cos 2\Psi \cos 2A + \cos 2(P-M) \cos 2M (\cos 2A - \cos 2\Psi) + \cos 2(P-M) \sin 2A \sin 2M \sin 2\Psi \cos \Delta$$

$$I_S = \sin 2(P-M) \sin 2A \sin 2\Psi \sin \Delta$$

$$I_C = \sin 2(P-M) [\sin 2M (\cos 2\Psi - \cos 2A) + \sin 2A \cos 2M \sin 2\Psi \cos \Delta]$$



# Phase Modulation Formalism

---

## ▪ 2 Common Measurement Configurations

- Configuration II: P – M=45 [90]; M = 0 [90]; A = 45 [90]

→  $I_s = \sin 2\Psi \sin \Delta$

$I_c = \sin 2\Psi \cos \Delta$

→ Accurate measurement of  $\Delta$  over [0-360°]

- Configuration III: P – M=45 [90]; M = 45 [90]; A = 45 [90]

→  $I_s = \sin 2\Psi \sin \Delta$

$I_{c'} = \cos 2\Psi$

→ Accurate measurement of  $\Psi$  over [0-90°]

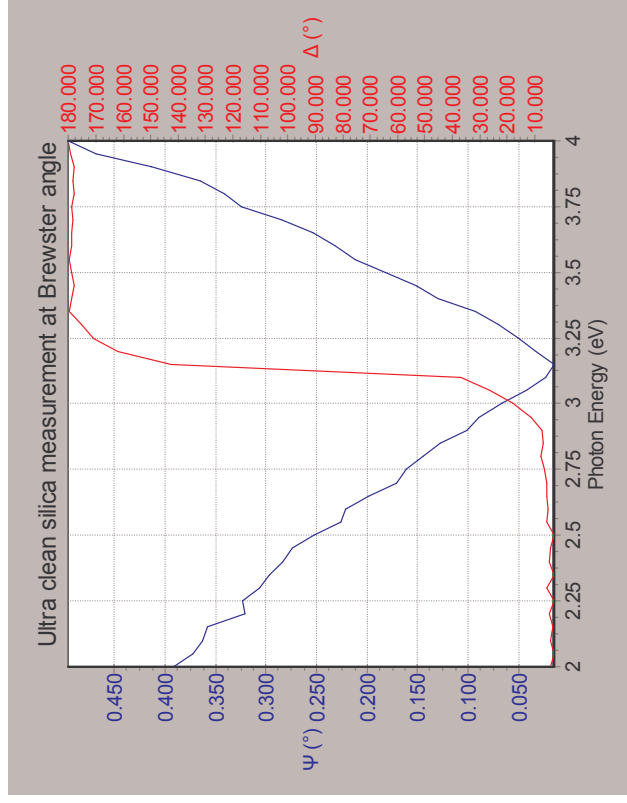
## ▪ Depolarization Measurement

- Given by:  $P = (I_s)^2 + (I_{c'})^2$
- $P=1$ : the sample is not depolarizing
- $P<1$ : the sample is depolarizing

# High Accuracy, High Sensitivity Phase Modulation Ellipsometer

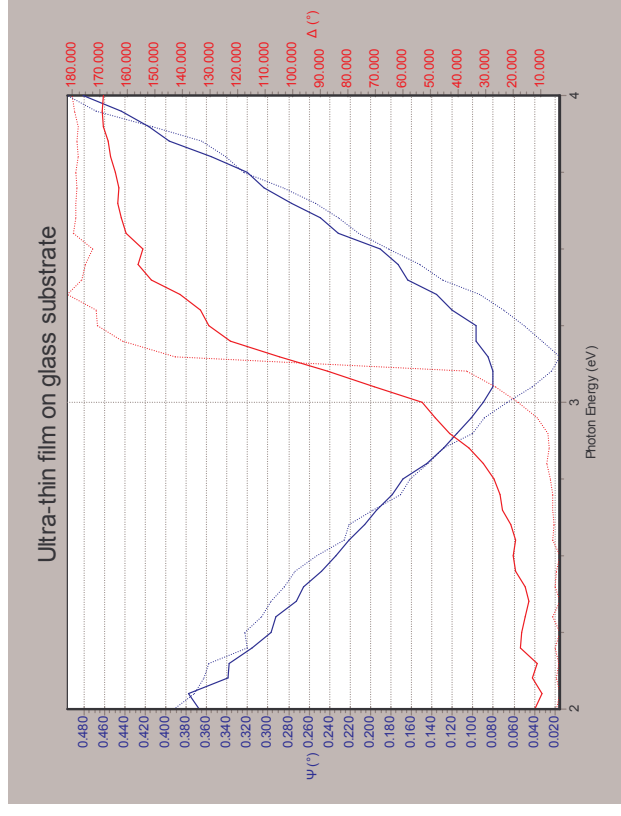
→ Accurate measurement of  $\Delta$  parameter around 0 & 180°

→ High sensitivity to ultra-thin films



Measurement of silica substrate at the Brewster angle

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10 Å monolayer deposition on silica substrate

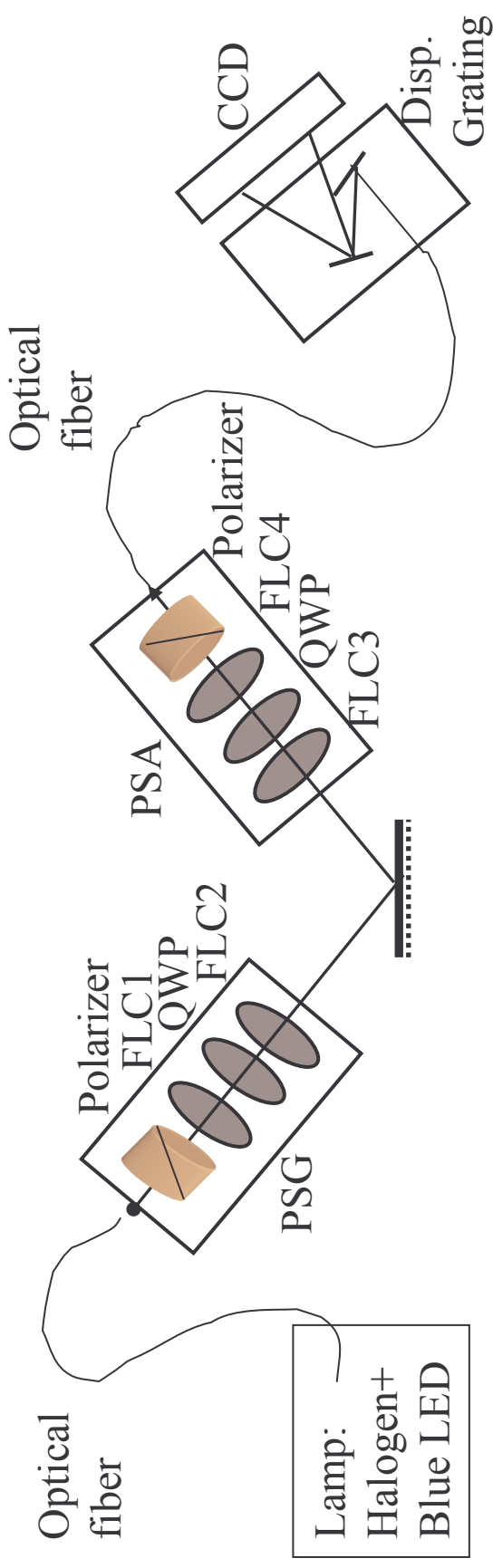
--- Ultra-thin monolayer  
— Silica substrate

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# Liquid Crystal Modulation Spectroscopic Ellipsometer

## Optical Set-up



### > Input and output heads are symmetrical

- Polarizer
- LC Modulator – states  $0^\circ$  and  $45^\circ$
- Quarter Waveplate
- LC Modulator – states  $0^\circ$  and  $45^\circ$

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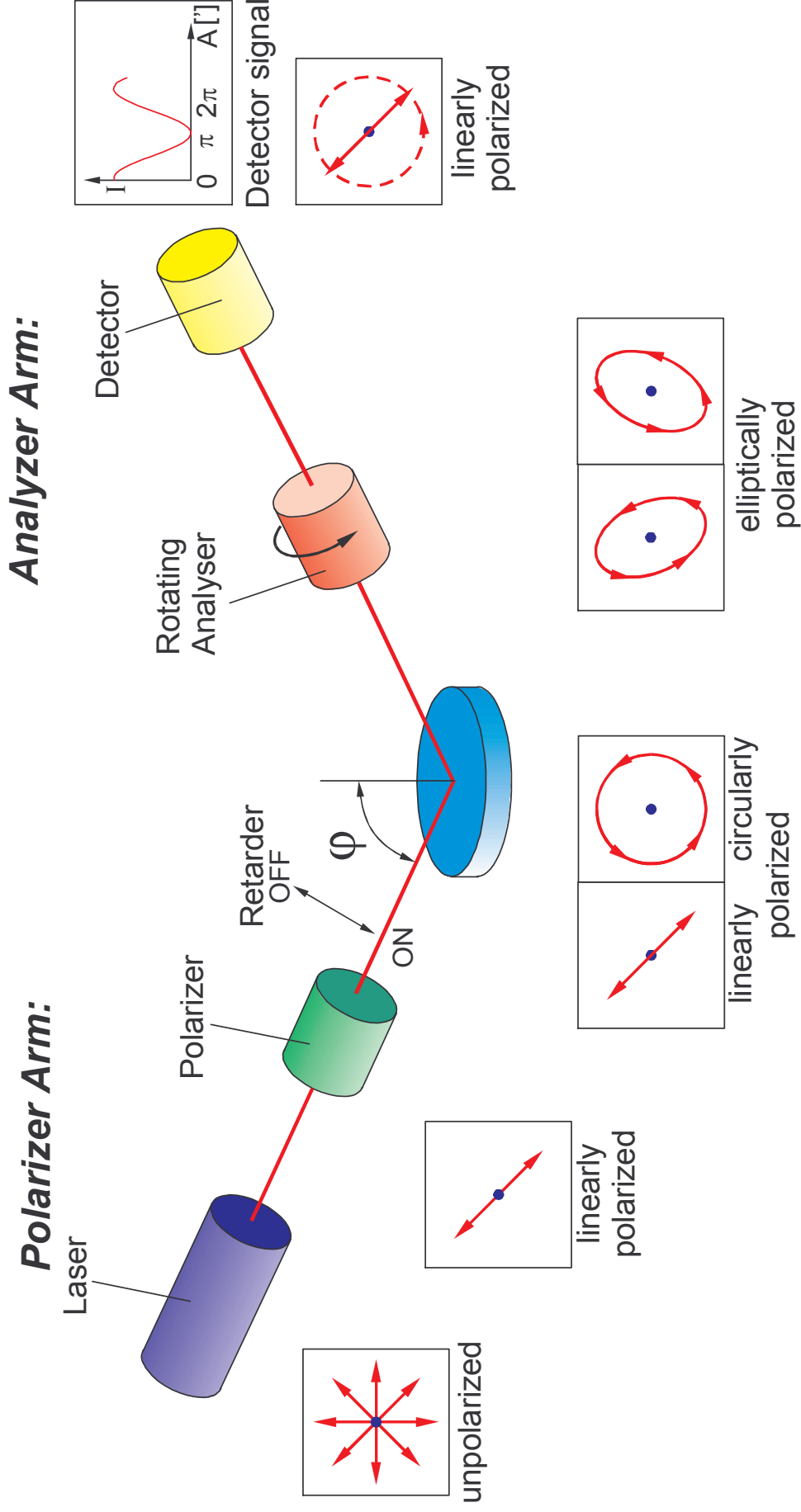
**MM-16**

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# Laser Ellipsometer

## Optical Set-up



**PZ2000**

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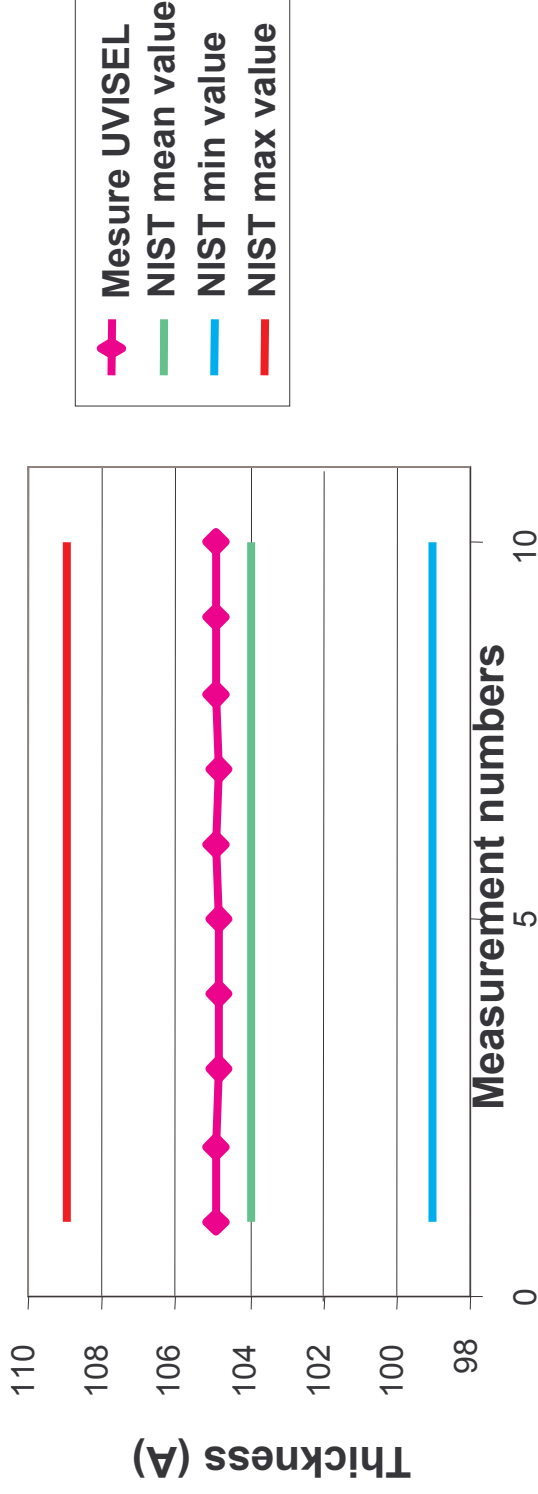
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# Ellipsometer Accuracy

- **Reference standards NIST**

- Check the good working of the ellipsometer by measuring one time per week your standard sample.



- **Straight-through air measurements**

- The only material for which the ellipsometric parameters are absolutely known is “Air”
- An ellipsometric measurement in the straight-through configuration should be by definition return  $\Psi=45^\circ$  and  $\Delta=0^\circ$

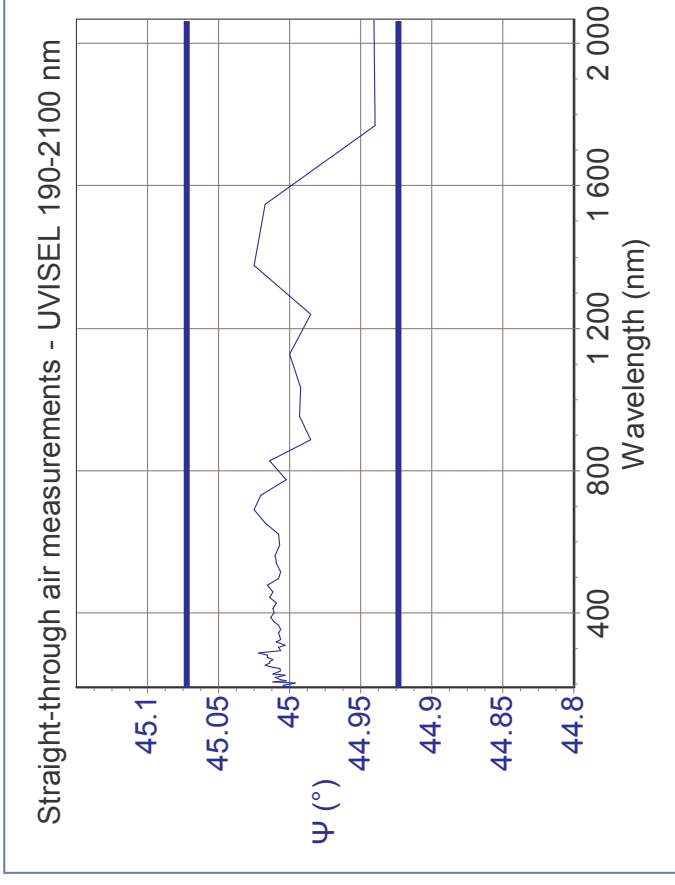
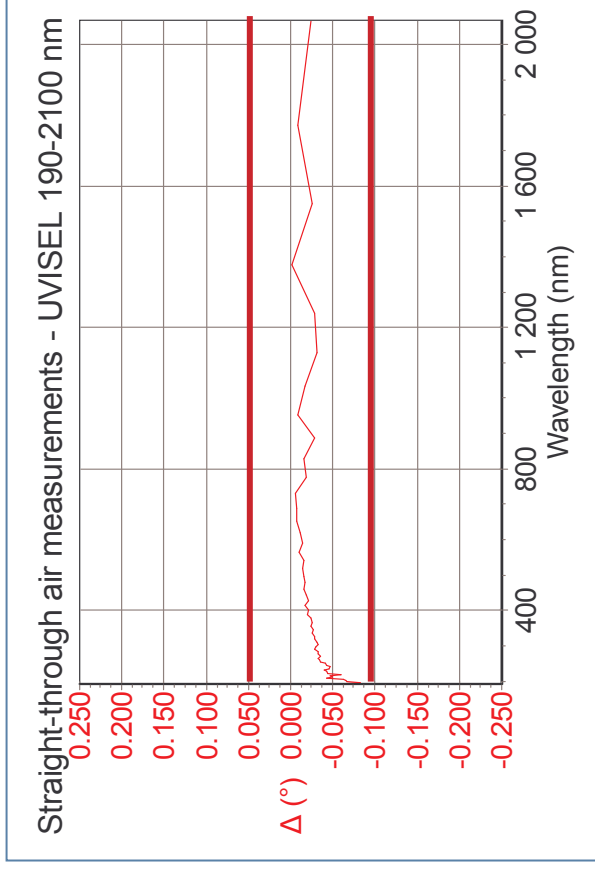
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# Ellipsometer Accuracy

## Straight-through air measurements



- **HJY UVISEL Specifications**

➔  $\Delta = 0^\circ \pm 0.083^\circ$

– Spectral range: 190 – 2100 nm

- **HJY UVISEL Specifications**

➔  $\Psi = 45^\circ \pm 0.06^\circ$

– Spectral range: 190 – 2100 nm

# Setting up Ellipsometric Measurement

## Spectral range

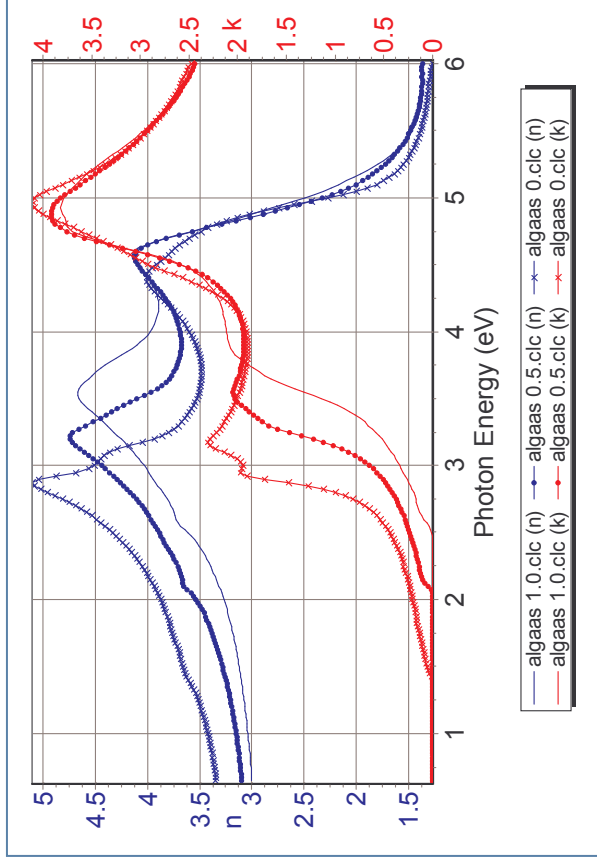
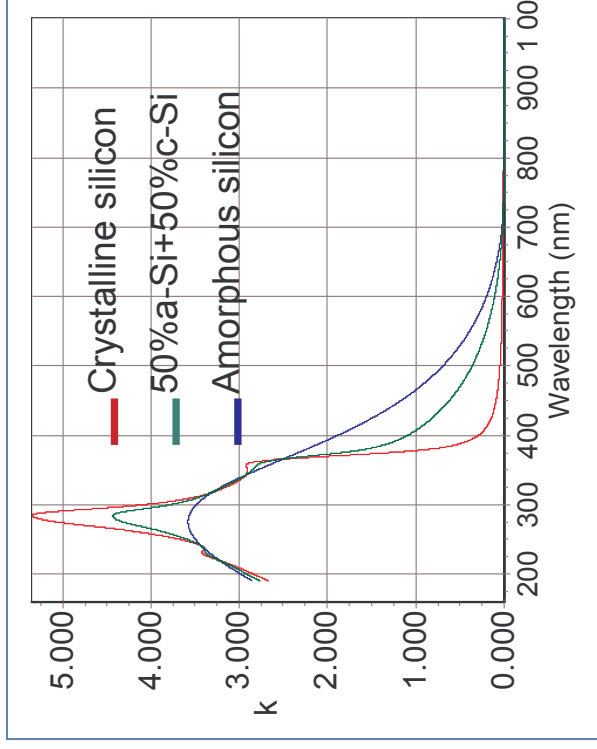
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- **What are your materials ?**
  - Semiconductor: transparent in NIR, strongly absorbing in VIS-FUV
  - Dielectric: transparent, absorbing in the FUV
  - Metal: strongly absorbing from NIR to FUV, especially in NIR
- **Which properties of interest ?**
  - Thickness
  - Optical constants
  - Material properties: composition, crystallinity...
- **Final applications**
  - Telecommunications, data storage applications require NIR wavelengths
  - Lithography requires FUV wavelengths
  - Advanced applications may require a special spectral range to provide accurate results

# Spectral range



- ⇒ Transparent region: thickness characterization
- ⇒ Absorptive region: crystallinity, composition characterization



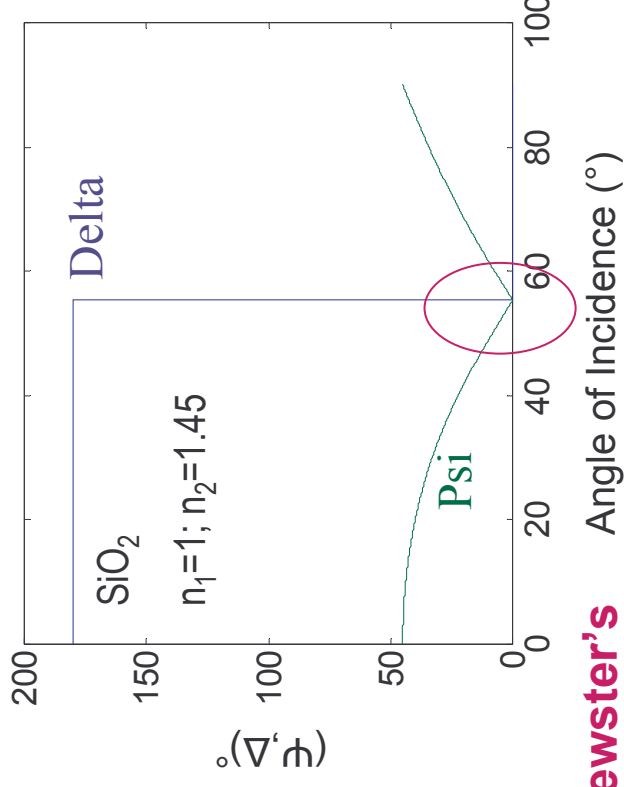
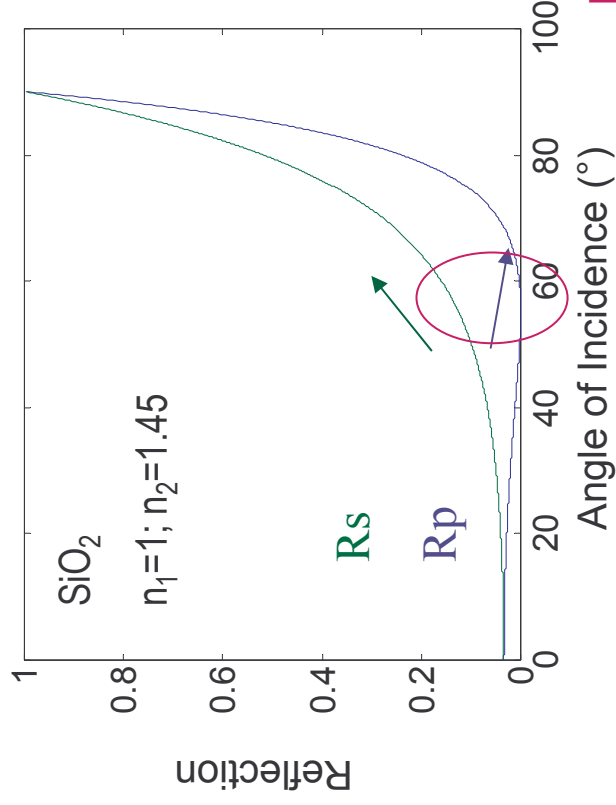
- Electronic transitions critical point broaden in amorphous materials

- Increasing Al increases the bandgap, which shifts the absorption edge to shorter  $\lambda$



# Angles of incidence

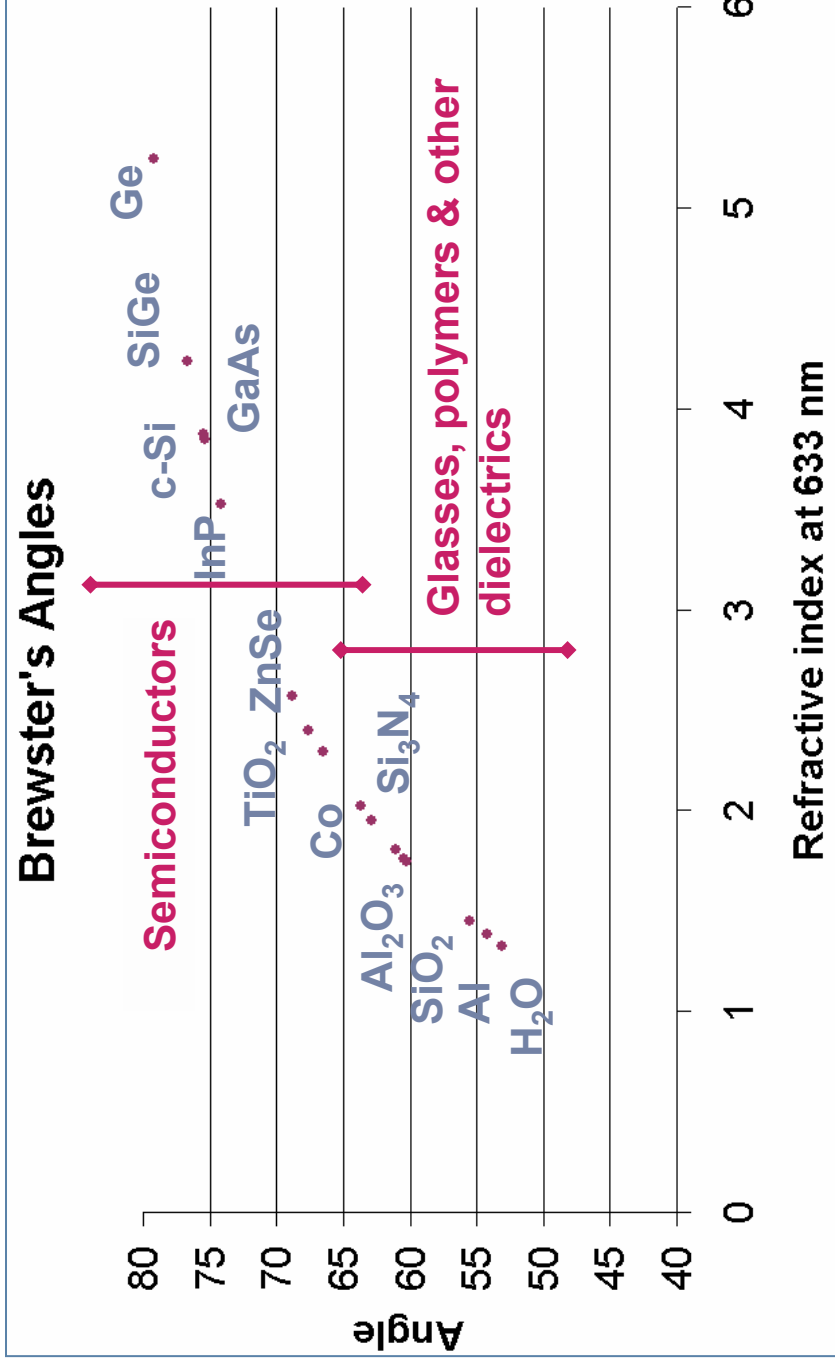
- Ellipsometry measurements are acquired at oblique angle of incidence
  - Why typically between  $50^\circ$  and  $80^\circ$  ?
    - To maximize the difference between s and p polarized light
- ⇒ **Brewster Angle**



# Brewster's Angles

⇒ Brewster angle defined by

$$\tan \phi_B = \frac{n_2}{n_1}$$



# Ellipsometry = Versatile Technology

## Overview of Applications Fields

---

- **Semiconductor** S
  - Transistors, memories, nanostructures...
- **Optoelectronic technologies** OT
  - Flat panel display, photovoltaic cells
- **Optical coatings** OC
  - ARC, electrochromic coating, auto-cleaning glass, mirror ...
- **Telecommunications** T
  - IR materials, data storage, non linear optical devices
- **Bio-Nano technology** BNT
  - Protein adsorption, SAM, surface chemistry, carbon nanotubes
- **Packaging** P
  - Barrier coating for food plastic film, bottles

# CONCLUSION

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- Why are Spectroscopic Ellipsometers powerful tools for materials characterization ?
  - Non destructive technique
  - Wide range of materials properties and excellent thickness resolution
  - Interesting correlation with many others techniques
  - Modular design
  - Robust technique for both research and industry